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Description Additional actuarial science functionality, mostly in the fields of loss distributions, risk theory (including ruin theory), simulation of compound hierarchical models and credibility theory. The package also features 17 new probability laws commonly used in insurance, most notably heavy tailed distributions.

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Imports stats, graphics

Suggests MASS

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adjCoef	<i>Adjustment Coefficient</i>
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Description

Compute the adjustment coefficient in ruin theory, or return a function to compute the adjustment coefficient for various reinsurance retentions.

Usage

```
adjCoef(mgf.claim, mgf.wait = mgfexp(x), premium.rate, upper.bound,
        h, reinsurance = c("none", "proportional", "excess-of-loss"),
        from, to, n = 101)
```

```
## S3 method for class 'adjCoef'
plot(x, xlab = "x", ylab = "R(x)",
     main = "Adjustment Coefficient", sub = comment(x),
     type = "l", add = FALSE, ...)
```

Arguments

mgf.claim	an expression written as a function of x or of x and y , or alternatively the name of a function, giving the moment generating function (mgf) of the claim severity distribution.
mgf.wait	an expression written as a function of x , or alternatively the name of a function, giving the mgf of the claims interarrival time distribution. Defaults to an exponential distribution with parameter 1.
premium.rate	if reinsurance = "none", a numeric value of the premium rate; otherwise, an expression written as a function of y , or alternatively the name of a function, giving the premium rate function.
upper.bound	numeric; an upper bound for the coefficient, usually the upper bound of the support of the claim severity mgf.
h	an expression written as a function of x or of x and y , or alternatively the name of a function, giving function h in the Lundberg equation (see below); ignored if mgf.claim is provided.
reinsurance	the type of reinsurance for the portfolio; can be abbreviated.
from, to	the range over which the adjustment coefficient will be calculated.

n	integer; the number of values at which to evaluate the adjustment coefficient.
x	an object of class "adjCoef".
xlab, ylab	label of the x and y axes, respectively.
main	main title.
sub	subtitle, defaulting to the type of reinsurance.
type	1-character string giving the type of plot desired; see plot for details.
add	logical; if TRUE add to already existing plot.
...	further graphical parameters accepted by plot or lines .

Details

In the typical case `reinsurance = "none"`, the coefficient of determination is the smallest (strictly) positive root of the Lundberg equation

$$h(x) = E[e^{xB-xcW}] = 1$$

on $[0, m)$, where $m = \text{upper.bound}$, B is the claim severity random variable, W is the claim interarrival (or wait) time random variable and $c = \text{premium.rate}$. The premium rate must satisfy the positive safety loading constraint $E[B - cW] < 0$.

With `reinsurance = "proportional"`, the equation becomes

$$h(x, y) = E[e^{xyB-xc(y)W}] = 1,$$

where y is the retention rate and $c(y)$ is the premium rate function.

With `reinsurance = "excess-of-loss"`, the equation becomes

$$h(x, y) = E[e^{x \min(B, y) - xc(y)W}] = 1,$$

where y is the retention limit and $c(y)$ is the premium rate function.

One can use argument `h` as an alternative way to provide function $h(x)$ or $h(x, y)$. This is necessary in cases where random variables B and W are not independent.

The root of $h(x) = 1$ is found by minimizing $(h(x) - 1)^2$.

Value

If `reinsurance = "none"`, a numeric vector of length one. Otherwise, a function of class "adjCoef" inheriting from the "function" class.

Author(s)

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References

- Bowers, N. J. J., Gerber, H. U., Hickman, J., Jones, D. and Nesbitt, C. (1986), *Actuarial Mathematics*, Society of Actuaries.
- Centeno, M. d. L. (2002), Measuring the effects of reinsurance by the adjustment coefficient in the Sparre-Anderson model, *Insurance: Mathematics and Economics* **30**, 37–49.
- Gerber, H. U. (1979), *An Introduction to Mathematical Risk Theory*, Huebner Foundation.
- Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
## Basic example: no reinsurance, exponential claim severity and wait
## times, premium rate computed with expected value principle and
## safety loading of 20%.
adjCoef(mgfexp, premium = 1.2, upper = 1)

## Same thing, giving function h.
h <- function(x) 1/((1 - x) * (1 + 1.2 * x))
adjCoef(h = h, upper = 1)

## Example 11.4 of Klugman et al. (2008)
mgfx <- function(x) 0.6 * exp(x) + 0.4 * exp(2 * x)
adjCoef(mgfx(x), mgfexp(x, 4), prem = 7, upper = 0.3182)

## Proportional reinsurance, same assumptions as above, reinsurer's
## safety loading of 30%.
mgfx <- function(x, y) mgfexp(x * y)
p <- function(x) 1.3 * x - 0.1
h <- function(x, a) 1/((1 - a * x) * (1 + x * p(a)))
R1 <- adjCoef(mgfx, premium = p, upper = 1, reins = "proportional",
             from = 0, to = 1, n = 11)
R2 <- adjCoef(h = h, upper = 1, reins = "p",
             from = 0, to = 1, n = 101)
R1(seq(0, 1, length = 10)) # evaluation for various retention rates
R2(seq(0, 1, length = 10)) # same
plot(R1) # graphical representation
plot(R2, col = "green", add = TRUE) # smoother function

## Excess-of-loss reinsurance
p <- function(x) 1.3 * levgamma(x, 2, 2) - 0.1
mgfx <- function(x, l)
  mgfgamma(x, 2, 2) * pgamma(l, 2, 2 - x) +
  exp(x * l) * pgamma(l, 2, 2, lower = FALSE)
h <- function(x, l) mgfx(x, l) * mgfexp(-x * p(l))
R1 <- adjCoef(mgfx, upper = 1, premium = p, reins = "excess-of-loss",
             from = 0, to = 10, n = 11)
R2 <- adjCoef(h = h, upper = 1, reins = "e",
             from = 0, to = 10, n = 101)
plot(R1)
plot(R2, col = "green", add = TRUE)
```

 aggregateDist

 Aggregate Claim Amount Distribution

Description

Compute the aggregate claim amount cumulative distribution function of a portfolio over a period using one of five methods.

Usage

```
aggregateDist(method = c("recursive", "convolution", "normal",
                        "npower", "simulation"),
             model.freq = NULL, model.sev = NULL, p0 = NULL,
             x.scale = 1, convolve = 0, moments, nb.simul, ...,
             tol = 1e-06, maxit = 500, echo = FALSE)

## S3 method for class 'aggregateDist'
print(x, ...)

## S3 method for class 'aggregateDist'
plot(x, xlim, ylab = expression(F[S](x)),
     main = "Aggregate Claim Amount Distribution",
     sub = comment(x), ...)

## S3 method for class 'aggregateDist'
summary(object, ...)

## S3 method for class 'aggregateDist'
mean(x, ...)

## S3 method for class 'aggregateDist'
diff(x, ...)
```

Arguments

method	method to be used
model.freq	for "recursive" method: a character string giving the name of a distribution in the $(a, b, 0)$ or $(a, b, 1)$ families of distributions. For "convolution" method: a vector of claim number probabilities. For "simulation" method: a frequency simulation model (see simul for details) or NULL. Ignored with normal and npower methods.
model.sev	for "recursive" and "convolution" methods: a vector of claim amount probabilities. For "simulation" method: a severity simulation model (see simul for details) or NULL. Ignored with normal and npower methods.
p0	arbitrary probability at zero for the frequency distribution. Creates a zero-modified or zero-truncated distribution if not NULL. Used only with "recursive" method.

x.scale	value of an amount of 1 in the severity model (monetary unit). Used only with "recursive" and "convolution" methods.
convolve	number of times to convolve the resulting distribution with itself. Used only with "recursive" method.
moments	vector of the true moments of the aggregate claim amount distribution; required only by the "normal" or "npower" methods.
nb.simul	number of simulations for the "simulation" method.
...	parameters of the frequency distribution for the "recursive" method; further arguments to be passed to or from other methods otherwise.
tol	the resulting cumulative distribution in the "recursive" method will get less than tol away from 1.
maxit	maximum number of recursions in the "recursive" method.
echo	logical; echo the recursions to screen in the "recursive" method.
x, object	an object of class "aggregateDist".
xlim	numeric of length 2; the x limits of the plot.
ylab	label of the y axis.
main	main title.
sub	subtitle, defaulting to the calculation method.

Details

aggregateDist returns a function to compute the cumulative distribution function (cdf) of the aggregate claim amount distribution in any point.

The "recursive" method computes the cdf using the Panjer algorithm; the "convolution" method using convolutions; the "normal" method using a normal approximation; the "npower" method using the Normal Power 2 approximation; the "simulation" method using simulations. More details follow.

Value

A function of class "aggregateDist", inheriting from the "function" class when using normal and Normal Power approximations and additionally inheriting from the "ecdf" and "stepfun" classes when other methods are used.

There are methods available to summarize (summary), represent (print), plot (plot), compute quantiles (quantile) and compute the mean (mean) of "aggregateDist" objects.

For the diff method: a numeric vector of probabilities corresponding to the probability mass function evaluated at the knots of the distribution.

Recursive method

The frequency distribution is a member of the $(a, b, 0)$ family of discrete distributions if p_0 is NULL and a member of the $(a, b, 1)$ family if p_0 is specified.

model.freq must be one of "binomial", "geometric", "negative binomial", "poisson" or "logarithmic" (these can abbreviated). The parameters of the frequency distribution must be

specified using names identical to the arguments of functions `dbinom`, `dgeom`, `dnbinom`, `dpois` and `dnbinom`, respectively. (The logarithmic distribution is a limiting case of the negative binomial distribution with size parameter equal to 0.)

`model.sev` is a vector of the (discretized) claim amount distribution X ; the first element **must** be $f_X(0) = \Pr[X = 0]$.

The recursion will fail to start if the expected number of claims is too large. One may divide the appropriate parameter of the frequency distribution by 2^n and convolve the resulting distribution $n = \text{convolve times}$.

Failure to obtain a cumulative distribution function less than `tol` away from 1 within `maxit` iterations is often due to a too coarse discretization of the severity distribution.

Convolution method

The cumulative distribution function (cdf) $F_S(x)$ of the aggregate claim amount of a portfolio in the collective risk model is

$$F_S(x) = \sum_{n=0}^{\infty} F_X^{*n}(x) p_n,$$

for $x = 0, 1, \dots$; $p_n = \Pr[N = n]$ is the frequency probability mass function and $F_X^{*n}(x)$ is the cdf of the n th convolution of the (discrete) claim amount random variable.

`model.freq` is vector p_n of the number of claims probabilities; the first element **must** be $\Pr[N = 0]$.

`model.sev` is vector $f_X(x)$ of the (discretized) claim amount distribution; the first element **must** be $f_X(0)$.

Normal and Normal Power 2 methods

The Normal approximation of a cumulative distribution function (cdf) $F(x)$ with mean μ and standard deviation σ is

$$F(x) \approx \Phi\left(\frac{x - \mu}{\sigma}\right).$$

The Normal Power 2 approximation of a cumulative distribution function (cdf) $F(x)$ with mean μ , standard deviation σ and skewness γ is

$$F(x) \approx \Phi\left(-\frac{3}{\gamma} + \sqrt{\frac{9}{\gamma^2} + 1 + \frac{6}{\gamma} \frac{x - \mu}{\sigma}}\right).$$

This formula is valid only for the right-hand tail of the distribution and skewness should not exceed unity.

Simulation method

This methods returns the empirical distribution function of a sample of size `nb.simul` of the aggregate claim amount distribution specified by `model.freq` and `model.sev`. `simul` is used for the simulation of claim amounts, hence both the frequency and severity models can be mixtures of distributions.

Author(s)

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References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Daykin, C.D., Pentikäinen, T. and Pesonen, M. (1994), *Practical Risk Theory for Actuaries*, Chapman & Hall.

See Also

[discretize](#) to discretize a severity distribution; [mean.aggregateDist](#) to compute the mean of the distribution; [quantile.aggregateDist](#) to compute the quantiles or the Value-at-Risk; [CTE.aggregateDist](#) to compute the Conditional Tail Expectation (or Tail Value-at-Risk); [simul](#).

Examples

```
## Convolution method (example 9.5 of Klugman et al. (2008))
fx <- c(0, 0.15, 0.2, 0.25, 0.125, 0.075,
        0.05, 0.05, 0.05, 0.025, 0.025)
pn <- c(0.05, 0.1, 0.15, 0.2, 0.25, 0.15, 0.06, 0.03, 0.01)
Fs <- aggregateDist("convolution", model.freq = pn,
                   model.sev = fx, x.scale = 25)

summary(Fs)
c(Fs(0), diff(Fs(25 * 0:21))) # probability mass function
plot(Fs)

## Recursive method
Fs <- aggregateDist("recursive", model.freq = "poisson",
                   model.sev = fx, lambda = 3, x.scale = 25)

plot(Fs)
Fs(knots(Fs)) # cdf evaluated at its knots
diff(Fs)      # probability mass function

## Recursive method (high frequency)
## Not run: Fs <- aggregateDist("recursive", model.freq = "poisson",
                              model.sev = fx, lambda = 1000)

## End(Not run)
Fs <- aggregateDist("recursive", model.freq = "poisson",
                   model.sev = fx, lambda = 250, convolve = 2, maxit = 1500)

plot(Fs)

## Normal Power approximation
Fs <- aggregateDist("npower", moments = c(200, 200, 0.5))
Fs(210)

## Simulation method
model.freq <- expression(data = rpois(3))
model.sev <- expression(data = rgamma(100, 2))
Fs <- aggregateDist("simulation", nb.simul = 1000,
```

```

                                model.freq, model.sev)
mean(Fs)
plot(Fs)

## Evaluation of ruin probabilities using Beekman's formula with
## Exponential(1) claim severity, Poisson(1) frequency and premium rate
## c = 1.2.
fx <- discretize(pexp(x, 1), from = 0, to = 100, method = "lower")
phi0 <- 0.2/1.2
Fs <- aggregateDist(method = "recursive", model.freq = "geometric",
                    model.sev = fx, prob = phi0)
1 - Fs(400) # approximate ruin probability
u <- 0:100
plot(u, 1 - Fs(u), type = "l", main = "Ruin probability")

```

BetaMoments

*Raw and Limited Moments of the Beta Distribution***Description**

Raw moments and limited moments for the (central) Beta distribution with parameters shape1 and shape2.

Usage

```
mbeta(order, shape1, shape2)
levbeta(limit, shape1, shape2, order = 1)
```

Arguments

order order of the moment.
limit limit of the loss variable.
shape1, shape2 positive parameters of the Beta distribution.

Details

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

The noncentral Beta distribution is not supported.

Value

mbeta gives the k th raw moment and levbeta gives the k th moment of the limited loss variable. Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

See Also

[Beta](#) for details on the Beta distribution and functions `{d,p,q,r}beta`.

Examples

```
mbeta(2, 3, 4) - mbeta(1, 3, 4)^2
levbeta(10, 3, 4, order = 2)
```

Burr

The Burr Distribution

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Burr distribution with parameters shape1, shape2 and scale.

Usage

```
dburr(x, shape1, shape2, rate = 1, scale = 1/rate,
      log = FALSE)
pburr(q, shape1, shape2, rate = 1, scale = 1/rate,
      lower.tail = TRUE, log.p = FALSE)
qburr(p, shape1, shape2, rate = 1, scale = 1/rate,
      lower.tail = TRUE, log.p = FALSE)
rburr(n, shape1, shape2, rate = 1, scale = 1/rate)
mburr(order, shape1, shape2, rate = 1, scale = 1/rate)
levburr(limit, shape1, shape2, rate = 1, scale = 1/rate,
        order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape1, shape2, scale</code>	parameters. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Burr distribution with parameters $\text{shape1} = \alpha$, $\text{shape2} = \gamma$ and $\text{scale} = \theta$ has density:

$$f(x) = \frac{\alpha\gamma(x/\theta)^\gamma}{x[1 + (x/\theta)^\gamma]^{\alpha+1}}$$

for $x > 0$, $\alpha > 0$, $\gamma > 0$ and $\theta > 0$.

The Burr is the distribution of the random variable

$$\theta \left(\frac{X}{1-X} \right)^{1/\gamma},$$

where X has a Beta distribution with parameters 1 and α .

The Burr distribution has the following special cases:

- A [Loglogistic](#) distribution when $\text{shape1} == 1$;
- A [Paralogistic](#) distribution when $\text{shape2} == \text{shape1}$;
- A [Pareto](#) distribution when $\text{shape2} == 1$.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)]$.

Value

`dburr` gives the density, `pburr` gives the distribution function, `qburr` gives the quantile function, `rburr` generates random deviates, `mburr` gives the k th raw moment, and `levburr` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Distribution also known as the Burr Type XII or Singh-Maddala distribution.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dburr(2, 3, 4, 5, log = TRUE))
p <- (1:10)/10
pburr(qburr(p, 2, 3, 1), 2, 3, 1)
mburr(2, 1, 2, 3) - mburr(1, 1, 2, 3) ^ 2
levburr(10, 1, 2, 3, order = 2)
```

ChisqSupp *Moments and Moment Generating Function of the (non-central) Chi-Squared Distribution*

Description

Raw moments, limited moments and moment generating function for the chi-squared (χ^2) distribution with `df` degrees of freedom and optional non-centrality parameter `ncp`.

Usage

```
mchisq(order, df, ncp = 0)
levchisq(limit, df, ncp = 0, order = 1)
mgfchisq(x, df, ncp = 0, log= FALSE)
```

Arguments

<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.
<code>df</code>	degrees of freedom (non-negative, but can be non-integer).
<code>ncp</code>	non-centrality parameter (non-negative).
<code>x</code>	numeric vector.
<code>log</code>	logical; if TRUE, the cumulant generating function is returned.

Details

The k th raw moment of the random variable X is $E[X^k]$, the k th limited moment at some limit d is $E[\min(X, d)^k]$ and the moment generating function is $E[e^{xX}]$.

Only integer moments are supported for the non central Chi-square distribution (`ncp > 0`).

The limited expected value is supported for the centered Chi-square distribution (`ncp = 0`).

Value

`mchisq` gives the k th raw moment, `levchisq` gives the k th moment of the limited loss variable, and `mgfchisq` gives the moment generating function in `x`.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Christophe Dutang, Vincent Goulet <vincent.goulet@act.ulaval.ca>

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Johnson, N. L. and Kotz, S. (1970), *Continuous Univariate Distributions, Volume 1*, Wiley.

See Also[Chisquare](#)**Examples**

```
mchisq(2, 3, 4)
levchisq(10, 3, order = 2)
mgfchisq(1, 3, 2)
```

cm

Credibility Models

Description

Fit the following credibility models: Bühlmann, Bühlmann-Straub, hierarchical or regression (Hachemeister).

Usage

```
cm(formula, data, ratios, weights, subset,
   regformula = NULL, regdata, adj.intercept = FALSE,
   method = c("Buhlmann-Gisler", "Ohlsson", "iterative"),
   tol = sqrt(.Machine$double.eps), maxit = 100, echo = FALSE)
```

```
## S3 method for class 'cm'
print(x, ...)
```

```
## S3 method for class 'cm'
predict(object, levels = NULL, newdata, ...)
```

```
## S3 method for class 'cm'
summary(object, levels = NULL, newdata, ...)
```

```
## S3 method for class 'summary.cm'
print(x, ...)
```

Arguments

formula	an object of class " <i>formula</i> ": a symbolic description of the model to be fit. The details of model specification are given below.
data	a matrix or a data frame containing the portfolio structure, the ratios or claim amounts and their associated weights, if any.
ratios	expression indicating the columns of data containing the ratios or claim amounts.
weights	expression indicating the columns of data containing the weights associated with ratios.

subset	an optional logical expression indicating a subset of observations to be used in the modeling process. All observations are included by default.
regformula	an object of class "formula": symbolic description of the regression component (see lm for details). No left hand side is needed in the formula; if present it is ignored. If NULL, no regression is done on the data.
regdata	an optional data frame, list or environment (or object coercible by as.data.frame to a data frame) containing the variables in the regression model.
adj.intercept	if TRUE, the intercept of the regression model is located at the barycenter of the regressor instead of the origin.
method	estimation method for the variance components of the model; see details below.
tol	tolerance level for the stopping criteria for iterative estimation method.
maxit	maximum number of iterations in iterative estimation method.
echo	logical; whether to echo the iterative procedure or not
x, object	an object of class "cm"
levels	character vector indicating the levels to predict or to include in the summary; if NULL all levels are included.
newdata	data frame containing the variables used to predict credibility regression models.
...	additional attributes to attach to the result for the predict and summary methods; further arguments to format for the print.summary method; unused for the print method.

Details

cm is the unified front end for credibility models fitting. Currently, the function supports hierarchical models with any number of levels (with Bühlmann and Bühlmann-Straub models as special cases) and the regression model of Hachemeister. Usage of cm is similar to [lm](#).

The formula argument symbolically describes the structure of the portfolio in the form $\sim terms$. Each term is an interaction between risk factors contributing to the total variance of the portfolio data. Terms are separated by + operators and interactions within each term by :. For a portfolio divided first into sectors, then units and finally contracts, formula would be $\sim sector + sector:unit + sector:unit:contract$, where sector, unit and contract are column names in data. In general, the formula should be of the form $\sim a + a:b + a:b:c + a:b:c:d + \dots$

If argument regformula is not NULL, the regression model of Hachemeister is fit to the data. The response is usually time. By default, the intercept of the model is located at time origin. If argument adj.intercept is TRUE, the intercept is moved to the (collective) barycenter of time, by orthogonalization of the design matrix. Note that the regression coefficients may be difficult to interpret in this case.

Arguments ratios, weights and subset are used like arguments select, select and subset, respectively, of function [subset](#).

Data does not have to be sorted by level. Nodes with no data (complete lines of NA except for the portfolio structure) are allowed, with the restriction mentioned above.

Value

Function `cm` computes the structure parameters estimators of the model specified in `formula`. The value returned is an object of class `cm`.

An object of class "`cm`" is a list with at least the following components:

<code>means</code>	a list containing, for each level, the vector of linearly sufficient statistics.
<code>weights</code>	a list containing, for each level, the vector of total weights.
<code>unbiased</code>	a vector containing the unbiased variance components estimators, or <code>NULL</code> .
<code>iterative</code>	a vector containing the iterative variance components estimators, or <code>NULL</code> .
<code>cred</code>	for multi-level hierarchical models: a list containing, the vector of credibility factors for each level. For one-level models: an array or vector of credibility factors.
<code>nodes</code>	a list containing, for each level, the vector of the number of nodes in the level.
<code>classification</code>	the columns of data containing the portfolio classification structure.
<code>ordering</code>	a list containing, for each level, the affiliation of a node to the node of the level above.

Regression fits have in addition the following components:

<code>adj.models</code>	a list containing, for each node, the credibility adjusted regression model as obtained with <code>lm.fit</code> or <code>lm.wfit</code> .
<code>transition</code>	if <code>adj.intercept</code> is <code>TRUE</code> , a transition matrix from the basis of the orthogonal design matrix to the basis of the original design matrix.
<code>terms</code>	the <code>terms</code> object used.

The method of `predict` for objects of class "`cm`" computes the credibility premiums for the nodes of every level included in `argument levels` (all by default). Result is a list the same length as `levels` or the number of levels in `formula`, or an atomic vector for one-level models.

Hierarchical models

The credibility premium at one level is a convex combination between the linearly sufficient statistic of a node and the credibility premium of the level above. (For the first level, the complement of credibility is given to the collective premium.) The linearly sufficient statistic of a node is the credibility weighted average of the data of the node, except at the last level, where natural weights are used. The credibility factor of node i is equal to

$$\frac{w_i}{w_i + a/b},$$

where w_i is the weight of the node used in the linearly sufficient statistic, a is the average within node variance and b is the average between node variance.

Regression models

The credibility premium of node i is equal to

$$y' b_i^a,$$

where y is a matrix created from newdata and b_i^a is the vector of credibility adjusted regression coefficients of node i . The latter is given by

$$b_i^a = Z_i b_i + (I - Z_i) m,$$

where b_i is the vector of regression coefficients based on data of node i only, m is the vector of collective regression coefficients, Z_i is the credibility matrix and I is the identity matrix. The credibility matrix of node i is equal to

$$A^{-1}(A + s^2 S_i),$$

where S_i is the unscaled regression covariance matrix of the node, s^2 is the average within node variance and A is the within node covariance matrix.

If the intercept is positioned at the barycenter of time, matrices S_i and A (and hence Z_i) are diagonal. This amounts to use Bühlmann-Straub models for each regression coefficient.

Argument newdata provides the “future” value of the regressors for prediction purposes. It should be given as specified in [predict.lm](#).

Variance components estimation

For hierarchical models, two sets of estimators of the variance components (other than the within node variance) are available: unbiased estimators and iterative estimators.

Unbiased estimators are based on sums of squares of the form

$$B_i = \sum_j w_{ij} (X_{ij} - \bar{X}_i)^2 - (J - 1)a$$

and constants of the form

$$c_i = w_i - \sum_j \frac{w_{ij}^2}{w_i},$$

where X_{ij} is the linearly sufficient statistic of level (ij) ; \bar{X}_i is the weighted average of the latter using weights w_{ij} ; $w_i = \sum_j w_{ij}$; J is the effective number of nodes at level (ij) ; a is the within variance of this level. Weights w_{ij} are the natural weights at the lowest level, the sum of the natural weights the next level and the sum of the credibility factors for all upper levels.

The Bühlmann-Gisler estimators (method = "Bühlmann-Gisler") are given by

$$b = \frac{1}{I} \sum_i \max\left(\frac{B_i}{c_i}, 0\right),$$

that is the average of the per node variance estimators truncated at 0.

The Ohlsson estimators (method = "Ohlsson") are given by

$$b = \frac{\sum_i B_i}{\sum_i c_i},$$

that is the weighted average of the per node variance estimators without any truncation. Note that negative estimates will be truncated to zero for credibility factor calculations.

In the Bühlmann-Straub model, these estimators are equivalent.

Iterative estimators method = "iterative" are pseudo-estimators of the form

$$b = \frac{1}{d} \sum_i w_i (X_i - \bar{X})^2,$$

where X_i is the linearly sufficient statistic of one level, \bar{X} is the linearly sufficient statistic of the level above and d is the effective number of nodes at one level minus the effective number of nodes of the level above. The Ohlsson estimators are used as starting values.

For regression models, with the intercept at time origin, only iterative estimators are available. If method is different from "iterative", a warning is issued. With the intercept at the barycenter of time, the choice of estimators is the same as in the Bühlmann-Straub model.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Xavier Milhaud, Tommy Ouellet, Louis-Philippe Pouliot

References

- Bühlmann, H. and Gisler, A. (2005), *A Course in Credibility Theory and its Applications*, Springer.
- Belhadj, H., Goulet, V. and Ouellet, T. (2009), On parameter estimation in hierarchical credibility, *Astin Bulletin* **39**.
- Goulet, V. (1998), Principles and application of credibility theory, *Journal of Actuarial Practice* **6**, ISSN 1064-6647.
- Goovaerts, M. J. and Hoogstad, W. J. (1987), *Credibility Theory*, Surveys of Actuarial Studies, No. 4, Nationale-Nederlanden N.V.

See Also

[subset](#), [formula](#), [lm](#), [predict.lm](#).

Examples

```
data(hachemeister)

## Buhlmann-Straub model
fit <- cm(~state, hachemeister,
         ratios = ratio.1:ratio.12, weights = weight.1:weight.12)
fit # print method
predict(fit) # credibility premiums
summary(fit) # more details

## Two-level hierarchical model. Notice that data does not have
## to be sorted by level
X <- data.frame(unit = c("A", "B", "A", "B", "B"), hachemeister)
fit <- cm(~unit + unit:state, X, ratio.1:ratio.12, weight.1:weight.12)
```

```

predict(fit)
predict(fit, levels = "unit") # unit credibility premiums only
summary(fit)
summary(fit, levels = "unit") # unit summaries only

## Regression model with intercept at time origin
fit <- cm(~state, hachemeister,
         regformula = ~time, regdata = data.frame(time = 12:1),
         ratios = ratio.1:ratio.12, weights = weight.1:weight.12)

fit
predict(fit, newdata = data.frame(time = 0))
summary(fit, newdata = data.frame(time = 0))

## Same regression model, with intercept at barycenter of time
fit <- cm(~state, hachemeister, adj.intercept = TRUE,
         regformula = ~time, regdata = data.frame(time = 12:1),
         ratios = ratio.1:ratio.12, weights = weight.1:weight.12)

fit
predict(fit, newdata = data.frame(time = 0))
summary(fit, newdata = data.frame(time = 0))

```

coverage

Density and Cumulative Distribution Function for Modified Data

Description

Compute probability density function or cumulative distribution function of the payment per payment or payment per loss random variable under any combination of the following coverage modifications: deductible, limit, coinsurance, inflation.

Usage

```

coverage(pdf, cdf, deductible = 0, franchise = FALSE,
         limit = Inf, coinsurance = 1, inflation = 0,
         per.loss = FALSE)

```

Arguments

pdf, cdf	function object or character string naming a function to compute, respectively, the probability density function and cumulative distribution function of a probability law.
deductible	a unique positive numeric value.
franchise	logical; TRUE for a franchise deductible, FALSE (default) for an ordinary deductible.
limit	a unique positive numeric value larger than deductible.
coinsurance	a unique value between 0 and 1; the proportion of coinsurance.
inflation	a unique value between 0 and 1; the rate of inflation.
per.loss	logical; TRUE for the per loss distribution, FALSE (default) for the per payment distribution.

Details

coverage returns a function to compute the probability density function (pdf) or the cumulative distribution function (cdf) of the distribution of losses under coverage modifications. The pdf and cdf of unmodified losses are pdf and cdf, respectively.

If pdf is specified, the pdf is returned; if pdf is missing or NULL, the cdf is returned. Note that cdf is needed if there is a deductible or a limit.

Value

An object of mode "function" with the same arguments as pdf or cdf, except "lower.tail", "log.p" and "log", which are not supported.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

See Also

vignette("coverage") for the exact definitions of the per payment and per loss random variables under an ordinary or franchise deductible.

Examples

```
## Default case: pdf of the per payment random variable with
## an ordinary deductible
coverage(dgamma, pgamma, deductible = 1)

## Add a limit
f <- coverage(dgamma, pgamma, deductible = 1, limit = 7)
f <- coverage("dgamma", "pgamma", deductible = 1, limit = 7) # same
f(0, shape = 3, rate = 1)
f(2, shape = 3, rate = 1)
f(6, shape = 3, rate = 1)
f(8, shape = 3, rate = 1)
curve(dgamma(x, 3, 1), xlim = c(0, 10), ylim = c(0, 0.3)) # original
curve(f(x, 3, 1), xlim = c(0.01, 5.99), col = 4, add = TRUE) # modified
points(6, f(6, 3, 1), pch = 21, bg = 4)

## Cumulative distribution function
F <- coverage(cdf = pgamma, deductible = 1, limit = 7)
F(0, shape = 3, rate = 1)
F(2, shape = 3, rate = 1)
F(6, shape = 3, rate = 1)
F(8, shape = 3, rate = 1)
curve(pgamma(x, 3, 1), xlim = c(0, 10), ylim = c(0, 1)) # original
curve(F(x, 3, 1), xlim = c(0, 5.99), col = 4, add = TRUE) # modified
```

```

curve(F(x, 3, 1), xlim = c(6, 10), col = 4, add = TRUE) # modified

## With no deductible, all distributions below are identical
coverage(dweibull, pweibull, limit = 5)
coverage(dweibull, pweibull, per.loss = TRUE, limit = 5)
coverage(dweibull, pweibull, franchise = TRUE, limit = 5)
coverage(dweibull, pweibull, per.loss = TRUE, franchise = TRUE,
        limit = 5)

## Coinsurance alone; only case that does not require the cdf
coverage(dgamma, coinsurance = 0.8)

```

CTE

Conditional Tail Expectation

Description

Conditional Tail Expectation, also called Tail Value-at-Risk.
TVaR is an alias for CTE.

Usage

```

CTE(x, ...)

## S3 method for class 'aggregateDist'
CTE(x, conf.level = c(0.9, 0.95, 0.99),
    names = TRUE, ...)

TVaR(x, ...)

```

Arguments

<code>x</code>	an R object.
<code>conf.level</code>	numeric vector of probabilities with values in $[0, 1)$.
<code>names</code>	logical; if true, the result has a <code>names</code> attribute. Set to FALSE for speedup with many probs.
<code>...</code>	further arguments passed to or from other methods.

Details

The Conditional Tail Expectation (or Tail Value-at-Risk) measures the average of losses above the Value at Risk for some given confidence level, that is $E[X|X > VaR(X)]$ where X is the loss random variable.

CTE is a generic function with, currently, only a method for objects of class "aggregateDist".

For the recursive, convolution and simulation methods of [aggregateDist](#), the CTE is computed from the definition using the empirical cdf.

For the normal approximation method, an explicit formula exists:

$$\mu + \frac{\sigma}{(1 - \alpha)} \sqrt{2\pi} e^{-\text{VaR}(X)^2/2},$$

where μ is the mean, σ the standard deviation and α the confidence level.

For the Normal Power approximation, the CTE is computed from the definition using [integrate](#).

Value

A numeric vector, named if names is TRUE.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Tommy Ouellet

See Also

[aggregateDist](#); [VaR](#)

Examples

```
model.freq <- expression(data = rpois(7))
model.sev <- expression(data = rnorm(9, 2))
Fs <- aggregateDist("simulation", model.freq, model.sev, nb.simul = 1000)
CTE(Fs)
```

dental

Individual Dental Claims Data Set

Description

Basic dental claims on a policy with a deductible of 50.

Usage

```
dental
```

Format

A vector containing 10 observations

Source

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

 discretize

Discretization of a Continuous Distribution

Description

Compute a discrete probability mass function from a continuous cumulative distribution function (cdf) with various methods.

discretise is an alias for discretize.

Usage

```
discretize(cdf, from, to, step = 1,
           method = c("upper", "lower", "rounding", "unbiased"),
           lev, by = step, xlim = NULL)
```

```
discretise(cdf, from, to, step = 1,
           method = c("upper", "lower", "rounding", "unbiased"),
           lev, by = step, xlim = NULL)
```

Arguments

cdf	an expression written as a function of x , or alternatively the name of a function, giving the cdf to discretize.
from, to	the range over which the function will be discretized.
step	numeric; the discretization step (or span, or lag).
method	discretization method to use.
lev	an expression written as a function of x , or alternatively the name of a function, to compute the limited expected value of the distribution corresponding to cdf. Used only with the "unbiased" method.
by	an alias for step.
xlim	numeric of length 2; if specified, it serves as default for <code>c(from, to)</code> .

Details

Usage is similar to [curve](#).

discretize returns the probability mass function (pmf) of the random variable obtained by discretization of the cdf specified in cdf.

Let $F(x)$ denote the cdf, $E[\min(X, x)]$ the limited expected value at x , h the step, p_x the probability mass at x in the discretized distribution and set $a = \text{from}$ and $b = \text{to}$.

Method "upper" is the forward difference of the cdf F :

$$p_x = F(x + h) - F(x)$$

for $x = a, a + h, \dots, b - \text{step}$.

Method "lower" is the backward difference of the cdf F :

$$p_x = F(x) - F(x - h)$$

for $x = a + h, \dots, b$ and $p_a = F(a)$.

Method "rounding" has the true cdf pass through the midpoints of the intervals $[x - h/2, x + h/2)$:

$$p_x = F(x + h/2) - F(x - h/2)$$

for $x = a + h, \dots, b - step$ and $p_a = F(a + h/2)$. The function assumes the cdf is continuous. Any adjustment necessary for discrete distributions can be done via `cdf`.

Method "unbiased" matches the first moment of the discretized and the true distributions. The probabilities are as follows:

$$p_a = \frac{E[\min(X, a)] - E[\min(X, a + h)]}{h} + 1 - F(a)$$

$$p_x = \frac{2E[\min(X, x)] - E[\min(X, x - h)] - E[\min(X, x + h)]}{h}, \quad a < x < b$$

$$p_b = \frac{E[\min(X, b)] - E[\min(X, b - h)]}{h} - 1 + F(b),$$

Value

A numeric vector of probabilities suitable for use in `aggregateDist`.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

See Also

[aggregateDist](#)

Examples

```
x <- seq(0, 5, 0.5)

op <- par(mfrow = c(1, 1), col = "black")

## Upper and lower discretization
fu <- discretize(pgamma(x, 1), method = "upper",
                from = 0, to = 5, step = 0.5)
fl <- discretize(pgamma(x, 1), method = "lower",
                from = 0, to = 5, step = 0.5)
curve(pgamma(x, 1), xlim = c(0, 5))
```

```

par(col = "blue")
plot(stepfun(head(x, -1), diffinv(fu)), pch = 19, add = TRUE)
par(col = "green")
plot(stepfun(x, diffinv(fl)), pch = 19, add = TRUE)
par(col = "black")

## Rounding (or midpoint) discretization
fr <- discretize(pgamma(x, 1), method = "rounding",
                from = 0, to = 5, step = 0.5)
curve(pgamma(x, 1), xlim = c(0, 5))
par(col = "blue")
plot(stepfun(head(x, -1), diffinv(fr)), pch = 19, add = TRUE)
par(col = "black")

## First moment matching
fb <- discretize(pgamma(x, 1), method = "unbiased",
                lev = levgamma(x, 1), from = 0, to = 5, step = 0.5)
curve(pgamma(x, 1), xlim = c(0, 5))
par(col = "blue")
plot(stepfun(x, diffinv(fb)), pch = 19, add = TRUE)

par(op)

```

elev

Empirical Limited Expected Value

Description

Compute the empirical limited expected value for individual or grouped data.

Usage

```

elev(x, ...)

## Default S3 method:
elev(x, ...)

## S3 method for class 'grouped.data'
elev(x, ...)

## S3 method for class 'elev'
print(x, digits = getOption("digits") - 2, ...)

## S3 method for class 'elev'
summary(object, ...)

## S3 method for class 'elev'
knots(Fn, ...)

```

```
## S3 method for class 'elev'
plot(x, ..., main = NULL, xlab = "x", ylab = "Empirical LEV")
```

Arguments

x a vector or an object of class "grouped.data" (in which case only the first column of frequencies is used); for the methods, an object of class "elev", typically.

digits number of significant digits to use, see [print](#).

Fn, object an R object inheriting from "ogive".

main main title.

xlab, ylab labels of x and y axis.

... arguments to be passed to subsequent methods.

Details

The limited expected value (LEV) at u of a random variable X is $E[X \wedge u] = E[\min(X, u)]$. For individual data x_1, \dots, x_n , the empirical LEV $E_n[X \wedge u]$ is thus

$$E_n[X \wedge u] = \frac{1}{n} \left(\sum_{x_j < u} x_j + \sum_{x_j \geq u} u \right).$$

Methods of `elev` exist for individual data or for grouped data created with `grouped.data`. The formula in this case is too long to show here. See the reference for details.

Value

For `elev`, a function of class "elev", inheriting from the "function" class.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

See Also

[grouped.data](#) to create grouped data objects; [stepfun](#) for related documentation (even though the empirical LEV is not a step function).

Examples

```

data(gdental)
lev <- elev(gdental)
lev
summary(lev)
knots(lev)          # the group boundaries

lev(knots(lev))     # empirical lev at boundaries
lev(c(80, 200, 2000)) # and at other limits

plot(lev, type = "o", pch = 16)

```

emm

*Empirical Moments***Description**

Raw empirical moments for individual and grouped data.

Usage

```

emm(x, order = 1, ...)

## Default S3 method:
emm(x, order = 1, ...)

## S3 method for class 'grouped.data'
emm(x, order = 1, ...)

```

Arguments

`x` a vector or matrix of individual data, or an object of class "grouped data".

`order` order of the moment. Must be positive.

`...` further arguments passed to or from other methods.

Details

Arguments `...` are passed to `colMeans`; `na.rm = TRUE` may be useful for individual data with missing values.

For individual data, the k th empirical moment is $\sum_{j=1}^n x_j^k$.

For grouped data with group boundaries c_1, \dots, c_r and group frequencies n_1, \dots, n_r , the k th empirical moment is

$$\sum_{j=1}^r \frac{n_j(c_j^k - c_{j-1}^k)}{n(k+1)(c_j - c_{j-1})},$$

where $n = \sum_{j=1}^r n_j$.

Value

A named vector or matrix of moments.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

See Also

[mean](#) and [mean.grouped.data](#) for simpler access to the first moment.

Examples

```
## Individual data
data(dental)
emm(dental, order = 1:3)

## Grouped data
data(gdental)
emm(gdental)
x <- grouped.data(cj = gdental[, 1],
                  nj1 = sample(1:100, nrow(gdental)),
                  nj2 = sample(1:100, nrow(gdental)))
emm(x) # same as mean(x)
```

ExponentialSupp

Moments and Moment Generating Function of the Exponential Distribution

Description

Raw moments, limited moments and moment generating function for the exponential distribution with rate rate (i.e., mean $1/\text{rate}$).

Usage

```
mexp(order, rate = 1)
levexp(limit, rate = 1, order = 1)
mgfexp(x, rate = 1, log = FALSE)
```

Arguments

order	order of the moment.
limit	limit of the loss variable.
rate	vector of rates.
x	numeric vector.
log	logical; if TRUE, the cumulant generating function is returned.

Details

The k th raw moment of the random variable X is $E[X^k]$, the k th limited moment at some limit d is $E[\min(X, d)^k]$ and the moment generating function is $E[e^{xX}]$.

Value

mexp gives the k th raw moment, levexp gives the k th moment of the limited loss variable, and mgfexp gives the moment generating function in x .

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Christophe Dutang and Mathieu Pigeon.

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Johnson, N. L. and Kotz, S. (1970), *Continuous Univariate Distributions, Volume 1*, Wiley.

See Also

[Exponential](#)

Examples

```
mexp(2, 3) - mexp(1, 3)^2
levexp(10, 3, order = 2)
mgfexp(1,2)
```

Extract.grouped.data *Extract or Replace Parts of a Grouped Data Object*

Description

Extract or replace subsets of grouped data objects.

Usage

```
## S3 method for class 'grouped.data'
x[i, j]
## S3 replacement method for class 'grouped.data'
x[i, j] <- value
```

Arguments

x	an object of class grouped.data.
i, j	elements to extract or replace. i, j are numeric or character or, for [only, empty. Numeric values are coerced to integer as if by as.integer . For replacement by [, a logical matrix is allowed, but not replacement in the group boundaries and group frequencies simultaneously.
value	a suitable replacement value.

Details

Objects of class "grouped.data" can mostly be indexed like data frames, with the following restrictions:

1. For [, the extracted object must keep a group boundaries column and at least one group frequencies column to remain of class "grouped.data";
2. For [<-, it is not possible to replace group boundaries and group frequencies simultaneously;
3. When replacing group boundaries, `length(value) == length(i) + 1`.

`x[, 1]` will return the plain vector of group boundaries.

Replacement of non adjacent group boundaries is not possible for obvious reasons.

Otherwise, extraction and replacement should work just like for data frames.

Value

For [an object of class "grouped.data", a data frame or a vector.

For [<- an object of class "grouped.data".

Note

Currently [[, [[<-, \$ and \$<- are not specifically supported, but should work as usual on group frequency columns.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>

See Also

[\[.data.frame\]](#) for extraction and replacement methods of data frames, [grouped.data](#) to create grouped data objects.

Examples

```
data(gdental)

(x <- gdental[1])      # select column 1
class(x)              # no longer a grouped.data object
class(gdental[2])     # same
gdental[, 1]          # group boundaries
gdental[, 2]          # group frequencies

gdental[1:4,]         # a subset
gdental[c(1, 3, 5),] # avoid this

gdental[1:2, 1] <- c(0, 30, 60) # modified boundaries
gdental[, 2] <- 10              # modified frequencies
## Not run: gdental[1, ] <- 2   # not allowed
```

GammaSupp

Moments and Moment Generating Function of the Gamma Distribution

Description

Raw moments, limited moments and moment generating function for the Gamma distribution with parameters shape and scale.

Usage

```
mgamma(order, shape, rate = 1, scale = 1/rate)
levgamma(limit, shape, rate = 1, scale = 1/rate, order = 1)
mgfgamma(x, shape, rate = 1, scale = 1/rate, log = FALSE)
```

Arguments

order	order of the moment.
limit	limit of the loss variable.
rate	an alternative way to specify the scale.
shape, scale	shape and scale parameters. Must be strictly positive.
x	numeric vector.
log	logical; if TRUE, the cumulant generating function is returned.

Details

The k th raw moment of the random variable X is $E[X^k]$, the k th limited moment at some limit d is $E[\min(X, d)^k]$ and the moment generating function is $E[e^{xX}]$.

Value

`mgamma` gives the k th raw moment, `levgamma` gives the k th moment of the limited loss variable, and `mgfgamma` gives the moment generating function in x .

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Christophe Dutang and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Johnson, N. L. and Kotz, S. (1970), *Continuous Univariate Distributions, Volume 1*, Wiley.

See Also

[GammaDist](#)

Examples

```
mgamma(2, 3, 4) - mgamma(1, 3, 4)^2
levgamma(10, 3, 4, order = 2)
mgfgamma(1, 3, 2)
```

gdental

Grouped Dental Claims Data Set

Description

Grouped dental claims, that is presented in a number of claims per claim amount group form.

Usage

```
gdental
```

Format

An object of class "grouped.data" (inheriting from class "data.frame") consisting of 10 rows and 2 columns. The environment of the object contains the plain vector of `cj` of group boundaries

Source

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

See Also

[grouped.data](#) for a description of grouped data objects.

 GeneralizedBeta

The Generalized Beta Distribution

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Generalized Beta distribution with parameters shape1, shape2, shape3 and scale.

Usage

```
dgenbeta(x, shape1, shape2, shape3, rate = 1, scale = 1/rate,
         log = FALSE)
pgenbeta(q, shape1, shape2, shape3, rate = 1, scale = 1/rate,
         lower.tail = TRUE, log.p = FALSE)
qgenbeta(p, shape1, shape2, shape3, rate = 1, scale = 1/rate,
         lower.tail = TRUE, log.p = FALSE)
rgenbeta(n, shape1, shape2, shape3, rate = 1, scale = 1/rate)
mgenbeta(order, shape1, shape2, shape3, rate = 1, scale = 1/rate)
levgenbeta(limit, shape1, shape2, shape3, rate = 1, scale = 1/rate,
           order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape1, shape2, shape3, scale</code>	parameters. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Generalized Beta distribution with parameters $\text{shape1} = \alpha$, $\text{shape2} = \beta$, $\text{shape3} = \tau$ and $\text{scale} = \theta$, has density:

$$f(x) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} (x/\theta)^{\alpha\tau} (1 - (x/\theta)^\tau)^{\beta-1} \frac{\tau}{x}$$

for $0 < x < \theta$, $\alpha > 0$, $\beta > 0$, $\tau > 0$ and $\theta > 0$. (Here $\Gamma(\alpha)$ is the function implemented by R's `gamma()` and defined in its help.)

The Generalized Beta is the distribution of the random variable

$$\theta X^{1/\tau},$$

where X has a Beta distribution with parameters α and β .

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)]$.

Value

`dgenbeta` gives the density, `pgenbeta` gives the distribution function, `qgenbeta` gives the quantile function, `rgenbeta` generates random deviates, `mgenbeta` gives the k th raw moment, and `levgenbeta` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

This is *not* the generalized three-parameter beta distribution defined on page 251 of Johnson et al, 1995.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Johnson, N. L., Kotz, S. and Balakrishnan, N. (1995) *Continuous Univariate Distributions, Volume 2*, Wiley.

Examples

```
exp(dgenbeta(2, 2, 3, 4, 0.2, log = TRUE))
p <- (1:10)/10
pgenbeta(qgenbeta(p, 2, 3, 4, 0.2), 2, 3, 4, 0.2)
mgenbeta(2, 1, 2, 3, 0.25) - mgenbeta(1, 1, 2, 3, 0.25) ^ 2
levgenbeta(10, 1, 2, 3, 0.25, order = 2)
```

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Generalized Pareto distribution with parameters shape1, shape2 and scale.

Usage

```
dgenpareto(x, shape1, shape2, rate = 1, scale = 1/rate,
           log = FALSE)
pgenpareto(q, shape1, shape2, rate = 1, scale = 1/rate,
           lower.tail = TRUE, log.p = FALSE)
qgenpareto(p, shape1, shape2, rate = 1, scale = 1/rate,
           lower.tail = TRUE, log.p = FALSE)
rgenpareto(n, shape1, shape2, rate = 1, scale = 1/rate)
mgenpareto(order, shape1, shape2, rate = 1, scale = 1/rate)
levgenpareto(limit, shape1, shape2, rate = 1, scale = 1/rate,
             order = 1)
```

Arguments

x, q	vector of quantiles.
p	vector of probabilities.
n	number of observations. If length(n) > 1, the length is taken to be the number required.
shape1, shape2, scale	parameters. Must be strictly positive.
rate	an alternative way to specify the scale.
log, log.p	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
order	order of the moment.
limit	limit of the loss variable.

Details

The Generalized Pareto distribution with parameters shape1 = α , shape2 = τ and scale = θ has density:

$$f(x) = \frac{\Gamma(\alpha + \tau)}{\Gamma(\alpha)\Gamma(\tau)} \frac{\theta^\alpha x^{\tau-1}}{(x + \theta)^{\alpha+\tau}}$$

for $x > 0$, $\alpha > 0$, $\tau > 0$ and $\theta > 0$. (Here $\Gamma(\alpha)$ is the function implemented by R's [gamma\(\)](#) and defined in its help.)

The Generalized Pareto is the distribution of the random variable

$$\theta \left(\frac{X}{1-X} \right),$$

where X has a Beta distribution with parameters α and τ .

The Generalized Pareto distribution has the following special cases:

- A [Pareto](#) distribution when `shape2 == 1`;
- An [Inverse Pareto](#) distribution when `shape1 == 1`.

Value

`dgenpareto` gives the density, `pgenpareto` gives the distribution function, `qgenpareto` gives the quantile function, `rgenpareto` generates random deviates, `mgenpareto` gives the k th raw moment, and `levgenpareto` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Distribution also known as the Beta of the Second Kind.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dgenpareto(3, 3, 4, 4, log = TRUE))
p <- (1:10)/10
pgenpareto(qgenpareto(p, 3, 3, 1), 3, 3, 1)
qgenpareto(.3, 3, 4, 4, lower.tail = FALSE)
mgenpareto(1, 3, 2, 1) ^ 2
levgenpareto(10, 3, 3, 3, order = 2)
```

grouped.data	<i>Grouped data</i>
--------------	---------------------

Description

Creation of grouped data objects, allowing for consistent representation and manipulation of data presented in a frequency per group form.

Usage

```
grouped.data(..., right = TRUE, row.names = NULL, check.rows = FALSE,  
             check.names = TRUE)
```

Arguments

... these arguments are either of the form `value` or `tag = value`. See Details.
right logical, indicating if the intervals should be closed on the right (and open on the left) or vice versa.
row.names, check.rows, check.names arguments identical to those of [data.frame](#).

Details

A grouped data object is a special form of data frame consisting of:

1. one column of contiguous group boundaries;
2. one or more columns of frequencies within each group.

The first argument will be taken as the vector of group boundaries. This vector must be exactly one element longer than the other arguments, which will be taken as vectors of group frequencies. All arguments are coerced to data frames.

Missing (NA) frequencies are replaced by zeros, with a warning.

Extraction and replacement methods exist for grouped.data objects, but working on non adjacent groups will most likely yield useless results.

Value

An object of class `c("grouped.data", "data.frame")` with an environment containing the vector `cj` of group boundaries.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Mathieu Pigeon and Louis-Philippe Pouliot

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

See Also

[\[.grouped.data\]](#) for extraction and replacement methods, [data.frame](#) for usual data frame creation and manipulation.

Examples

```
## Most common usage
cj <- c(0, 25, 50, 100, 250, 500, 1000)
nj <- c(30, 31, 57, 42, 45, 10)
(x <- grouped.data(Group = cj, Frequency = nj))
class(x)

x[, 1] # group boundaries
x[, 2] # group frequencies

## Multiple frequency columns are supported
x <- sample(1:100, 9)
y <- sample(1:100, 9)
grouped.data(cj = 1:10, nj.1 = x, nj.2 = y)
```

hachemeister

Hachemeister Data Set

Description

Hachemeister (1975) data set giving average claim amounts in private passenger bodily injury insurance in five U.S. states over 12 quarters between July 1970 and June 1973 and the corresponding number of claims.

Usage

```
hachemeister
```

Format

A matrix with 5 rows and the following 25 columns:

state the state number;

ratio.1,...,ratio.12 the average claim amounts;

weight.1,...,weight.12 the corresponding number of claims.

Source

Hachemeister, C. A. (1975), *Credibility for regression models with application to trend*, Proceedings of the Berkeley Actuarial Research Conference on Credibility, Academic Press.

hist.grouped.data *Histogram for Grouped Data*

Description

This method for the generic function `hist` is mainly useful to plot the histogram of grouped data. If `plot = FALSE`, the resulting object of class "histogram" is returned for compatibility with `hist.default`, but does not contain much information not already in `x`.

Usage

```
## S3 method for class 'grouped.data'
hist(x, freq = NULL, probability = !freq,
     density = NULL, angle = 45, col = NULL, border = NULL,
     main = paste("Histogram of" , xname),
     xlim = range(cj), ylim = NULL, xlab = xname, ylab,
     axes = TRUE, plot = TRUE, labels = FALSE, ...)
```

Arguments

<code>x</code>	an object of class "grouped.data"; only the first column of frequencies is used.
<code>freq</code>	logical; if TRUE, the histogram graphic is a representation of frequencies, the counts component of the result; if FALSE, probability densities, component density, are plotted (so that the histogram has a total area of one). Defaults to TRUE <i>iff</i> group boundaries are equidistant (and probability is not specified).
<code>probability</code>	an <i>alias</i> for <code>!freq</code> , for S compatibility.
<code>density</code>	the density of shading lines, in lines per inch. The default value of NULL means that no shading lines are drawn. Non-positive values of <code>density</code> also inhibit the drawing of shading lines.
<code>angle</code>	the slope of shading lines, given as an angle in degrees (counter-clockwise).
<code>col</code>	a colour to be used to fill the bars. The default of NULL yields unfilled bars.
<code>border</code>	the color of the border around the bars. The default is to use the standard foreground color.
<code>main, xlab, ylab</code>	these arguments to <code>title</code> have useful defaults here.
<code>xlim, ylim</code>	the range of <code>x</code> and <code>y</code> values with sensible defaults. Note that <code>xlim</code> is <i>not</i> used to define the histogram (breaks), but only for plotting (when <code>plot = TRUE</code>).
<code>axes</code>	logical. If TRUE (default), axes are draw if the plot is drawn.
<code>plot</code>	logical. If TRUE (default), a histogram is plotted, otherwise a list of breaks and counts is returned.
<code>labels</code>	logical or character. Additionally draw labels on top of bars, if not FALSE; see <code>plot.histogram</code> .
<code>...</code>	further graphical parameters passed to <code>plot.histogram</code> and their to <code>title</code> and <code>axis</code> (if <code>plot=TRUE</code>).

Value

An object of class "histogram" which is a list with components:

breaks	the $r + 1$ group boundaries.
counts	r integers; the frequency within each group.
density	the relative frequencies within each group n_j/n , where $n_j = \text{counts}[j]$.
intensities	same as density. Deprecated, but retained for compatibility.
mids	the r group midpoints.
xname	a character string with the actual x argument name.
equidist	logical, indicating if the distances between breaks are all the same.

Note

The resulting value does *not* depend on the values of the arguments `freq` (or `probability`) or `plot`. This is intentionally different from `S`.

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

See Also

[hist](#) and [hist.default](#) for histograms of individual data and fancy examples.

Examples

```
data(gdental)
hist(gdental)
```

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Inverse Burr distribution with parameters `shape1`, `shape2` and `scale`.

Usage

```

dinvburr(x, shape1, shape2, rate = 1, scale = 1/rate,
         log = FALSE)
pinvburr(q, shape1, shape2, rate = 1, scale = 1/rate,
         lower.tail = TRUE, log.p = FALSE)
qinvburr(p, shape1, shape2, rate = 1, scale = 1/rate,
         lower.tail = TRUE, log.p = FALSE)
rinvburr(n, shape1, shape2, rate = 1, scale = 1/rate)
minvburr(order, shape1, shape2, rate = 1, scale = 1/rate)
levinvburr(limit, shape1, shape2, rate = 1, scale = 1/rate,
           order = 1)

```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape1, shape2, scale</code>	parameters. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Inverse Burr distribution with parameters $\text{shape1} = \tau$, $\text{shape2} = \gamma$ and $\text{scale} = \theta$, has density:

$$f(x) = \frac{\tau\gamma(x/\theta)^{\gamma\tau}}{x[1 + (x/\theta)^\gamma]^{\tau+1}}$$

for $x > 0$, $\tau > 0$, $\gamma > 0$ and $\theta > 0$.

The Inverse Burr is the distribution of the random variable

$$\theta \left(\frac{X}{1-X} \right)^{1/\gamma},$$

where X has a Beta distribution with parameters τ and 1.

The Inverse Burr distribution has the following special cases:

- A [Loglogistic](#) distribution when $\text{shape1} == 1$;
- An [Inverse Pareto](#) distribution when $\text{shape2} == 1$;
- An [Inverse Paralogistic](#) distribution when $\text{shape1} == \text{shape2}$.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

dinvburr gives the density, invburr gives the distribution function, qinvburr gives the quantile function, rinvburr generates random deviates, minvburr gives the k th raw moment, and levinvburr gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Also known as the Dagum distribution.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dinvburr(2, 3, 4, 5, log = TRUE))
p <- (1:10)/10
pinvburr(qinvburr(p, 2, 3, 1), 2, 3, 1)
minvburr(2, 1, 2, 3) - minvburr(1, 1, 2, 3) ^ 2
levinvburr(10, 1, 2, 3, order = 2)
```

InverseExponential *The Inverse Exponential Distribution*

Description

Density function, distribution function, quantile function, random generation raw moments and limited moments for the Inverse Exponential distribution with parameter scale.

Usage

```
dinvexp(x, rate = 1, scale = 1/rate, log = FALSE)
pinvexp(q, rate = 1, scale = 1/rate, lower.tail = TRUE, log.p = FALSE)
qinvexp(p, rate = 1, scale = 1/rate, lower.tail = TRUE, log.p = FALSE)
rinvexp(n, rate = 1, scale = 1/rate)
minvexp(order, rate = 1, scale = 1/rate)
levinvexp(limit, rate = 1, scale = 1/rate, order)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>scale</code>	parameter. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Inverse Exponential distribution with parameter $\text{scale} = \theta$ has density:

$$f(x) = \frac{\theta e^{-\theta/x}}{x^2}$$

for $x > 0$ and $\theta > 0$.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

For numerical evaluation purposes, `levinvexp` requires that `order < 1`.

Value

`dinvexp` gives the density, `pinvexp` gives the distribution function, `qinvexp` gives the quantile function, `rinvexp` generates random deviates, `minvexp` gives the k th raw moment, and `levinvexp` calculates the k th limited moment.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dinvexp(2, 2, log = TRUE))
p <- (1:10)/10
pinvexp(qinvexp(p, 2), 2)
minvexp(0.5, 2)
```

Description

Density function, distribution function, quantile function, random generation, raw moments, and limited moments for the Inverse Gamma distribution with parameters shape and scale.

Usage

```
dinvgamma(x, shape, rate = 1, scale = 1/rate, log = FALSE)
pinvgamma(q, shape, rate = 1, scale = 1/rate,
           lower.tail = TRUE, log.p = FALSE)
qinvgamma(p, shape, rate = 1, scale = 1/rate,
           lower.tail = TRUE, log.p = FALSE)
rinvgamma(n, shape, rate = 1, scale = 1/rate)
minvgamma(order, shape, rate = 1, scale = 1/rate)
levinvgamma(limit, shape, rate = 1, scale = 1/rate,
            order = 1)
mgfinvgamma(x, shape, rate = 1, scale = 1/rate, log = FALSE)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape, scale</code>	parameters. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Inverse Gamma distribution with parameters $\text{shape} = \alpha$ and $\text{scale} = \theta$ has density:

$$f(x) = \frac{u^\alpha e^{-u}}{x\Gamma(\alpha)}, \quad u = \theta/x$$

for $x > 0$, $\alpha > 0$ and $\theta > 0$. (Here $\Gamma(\alpha)$ is the function implemented by R's `gamma()` and defined in its help.)

The special case `shape == 1` is an [Inverse Exponential](#) distribution.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

The moment generating function is given by $E[e^{xX}]$.

Value

dinvgamma gives the density, pinvgamma gives the distribution function, qinvgamma gives the quantile function, rinvgamma generates random deviates, minvgamma gives the k th raw moment, and levinvgamma gives the k th moment of the limited loss variable, mgfinvgamma gives the moment generating function in x .

Invalid arguments will result in return value NaN, with a warning.

Note

Also known as the Vinci distribution.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dinvgamma(2, 3, 4, log = TRUE))
p <- (1:10)/10
pinvgamma(qinvgamma(p, 2, 3), 2, 3)
minvgamma(-1, 2, 2) ^ 2
levinvgamma(10, 2, 2, order = 1)
mgfinvgamma(1,3,2)
```

InverseParalogistic *The Inverse Paralogistic Distribution*

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Inverse Paralogistic distribution with parameters shape and scale.

Usage

```
dinvparalogis(x, shape, rate = 1, scale = 1/rate, log = FALSE)
pinvparalogis(q, shape, rate = 1, scale = 1/rate,
              lower.tail = TRUE, log.p = FALSE)
qinvparalogis(p, shape, rate = 1, scale = 1/rate,
              lower.tail = TRUE, log.p = FALSE)
rinvparalogis(n, shape, rate = 1, scale = 1/rate)
minvparalogis(order, shape, rate = 1, scale = 1/rate)
levinvparalogis(limit, shape, rate = 1, scale = 1/rate,
                 order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape, scale</code>	parameters. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Inverse Paralogistic distribution with parameters $\text{shape} = \tau$ and $\text{scale} = \theta$ has density:

$$f(x) = \frac{\tau^2 (x/\theta)^{\tau^2}}{x[1 + (x/\theta)^\tau]^{\tau+1}}$$

for $x > 0$, $\tau > 0$ and $\theta > 0$.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`dinvparalogis` gives the density, `pinvparalogis` gives the distribution function, `qinvparalogis` gives the quantile function, `rinvparalogis` generates random deviates, `minvparalogis` gives the k th raw moment, and `levinvparalogis` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dinvparalogis(2, 3, 4, log = TRUE))
p <- (1:10)/10
pinvparalogis(qinvparalogis(p, 2, 3), 2, 3)
minvparalogis(-1, 2, 2)
levinvparalogis(10, 2, 2, order = 1)
```

Description

Density function, distribution function, quantile function, random generation raw moments and limited moments for the Inverse Pareto distribution with parameters shape and scale.

Usage

```
dinvpareto(x, shape, scale, log = FALSE)
pinvpareto(q, shape, scale, lower.tail = TRUE, log.p = FALSE)
qinvpareto(p, shape, scale, lower.tail = TRUE, log.p = FALSE)
rinvpareto(n, shape, scale)
minvpareto(order, shape, scale)
levinvpareto(limit, shape, scale, order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape, scale</code>	parameters. Must be strictly positive.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Inverse Pareto distribution with parameters $\text{shape} = \tau$ and $\text{scale} = \theta$ has density:

$$f(x) = \frac{\tau \theta x^{\tau-1}}{(x + \theta)^{\tau+1}}$$

for $x > 0$, $\tau > 0$ and $\theta > 0$.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Evaluation of `levinvpareto` is done using numerical integration.

Value

`dinvpareto` gives the density, `pinvpareto` gives the distribution function, `qinvpareto` gives the quantile function, `rinvpareto` generates random deviates, `minvpareto` gives the k th raw moment, and `levinvpareto` calculates the k th limited moment.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dinvpareto(2, 3, 4, log = TRUE))
p <- (1:10)/10
pinvpareto(qinvpareto(p, 2, 3), 2, 3)
minvpareto(0.5, 1, 2)
```

InverseTransformedGamma

The Inverse Transformed Gamma Distribution

Description

Density function, distribution function, quantile function, random generation, raw moments, and limited moments for the Inverse Transformed Gamma distribution with parameters shape1, shape2 and scale.

Usage

```
dinvtrgamma(x, shape1, shape2, rate = 1, scale = 1/rate,
            log = FALSE)
pinvtrgamma(q, shape1, shape2, rate = 1, scale = 1/rate,
            lower.tail = TRUE, log.p = FALSE)
qinvtrgamma(p, shape1, shape2, rate = 1, scale = 1/rate,
            lower.tail = TRUE, log.p = FALSE)
rinvtrgamma(n, shape1, shape2, rate = 1, scale = 1/rate)
minvtrgamma(order, shape1, shape2, rate = 1, scale = 1/rate)
levinvtrgamma(limit, shape1, shape2, rate = 1, scale = 1/rate,
            order = 1)
```

Arguments

x, q	vector of quantiles.
p	vector of probabilities.
n	number of observations. If length(n) > 1, the length is taken to be the number required.
shape1, shape2, scale	parameters. Must be strictly positive.

rate	an alternative way to specify the scale.
log, log.p	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
order	order of the moment.
limit	limit of the loss variable.

Details

The Inverse Transformed Gamma distribution with parameters $\text{shape1} = \alpha$, $\text{shape2} = \tau$ and $\text{scale} = \theta$, has density:

$$f(x) = \frac{\tau u^\alpha e^{-u}}{x \Gamma(\alpha)}, \quad u = (\theta/x)^\tau$$

for $x > 0$, $\alpha > 0$, $\tau > 0$ and $\theta > 0$. (Here $\Gamma(\alpha)$ is the function implemented by R's `gamma()` and defined in its help.)

The Inverse Transformed Gamma is the distribution of the random variable $\theta X^{-1/\tau}$, where X has a Gamma distribution with shape parameter α and scale parameter 1 or, equivalently, of the random variable $Y^{-1/\tau}$ with Y a Gamma distribution with shape parameter α and scale parameter $\theta^{-\tau}$.

The Inverse Transformed Gamma distribution defines a family of distributions with the following special cases:

- An [Inverse Gamma](#) distribution when $\text{shape2} == 1$;
- An [Inverse Weibull](#) distribution when $\text{shape1} == 1$;
- An [Inverse Exponential](#) distribution when $\text{shape1} == \text{shape2} == 1$;

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`dinvtrgamma` gives the density, `pinvtrgamma` gives the distribution function, `qinvtrgamma` gives the quantile function, `rinvtrgamma` generates random deviates, `minvtrgamma` gives the k th raw moment, and `levinvtrgamma` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Distribution also known as the Inverse Generalized Gamma.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dinvtrgamma(2, 3, 4, 5, log = TRUE))
p <- (1:10)/10
pinvtrgamma(qinvtrgamma(p, 2, 3, 4), 2, 3, 4)
minvtrgamma(2, 3, 4, 5)
levinvtrgamma(200, 3, 4, 5, order = 2)
```

InverseWeibull

The Inverse Weibull Distribution

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Inverse Weibull distribution with parameters shape and scale.

Usage

```
dinvweibull(x, shape, rate = 1, scale = 1/rate, log = FALSE)
pinvweibull(q, shape, rate = 1, scale = 1/rate,
            lower.tail = TRUE, log.p = FALSE)
qinvweibull(p, shape, rate = 1, scale = 1/rate,
            lower.tail = TRUE, log.p = FALSE)
rinvweibull(n, shape, rate = 1, scale = 1/rate)
minvweibull(order, shape, rate = 1, scale = 1/rate)
levinvweibull(limit, shape, rate = 1, scale = 1/rate,
              order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape, scale</code>	parameters. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Inverse Weibull distribution with parameters shape = τ and scale = θ has density:

$$f(x) = \frac{\tau(\theta/x)^\tau e^{-(\theta/x)^\tau}}{x}$$

for $x > 0$, $\tau > 0$ and $\theta > 0$.

The special case shape == 1 is an [Inverse Exponential](#) distribution.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

dinvweibull gives the density, pinvweibull gives the distribution function, qinvweibull gives the quantile function, rinvweibull generates random deviates, minvweibull gives the k th raw moment, and levinvweibull gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Distribution also know as the log-Gompertz.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dinvweibull(2, 3, 4, log = TRUE))
p <- (1:10)/10
pinvweibull(qinvweibull(p, 2, 3), 2, 3)
mlgompertz(-1, 3, 3)
levinvweibull(10, 2, 3, order = 2)
```

Description

Raw moments, limited moments and moment generating function for the Inverse Gaussian distribution with parameters nu and lambda.

Usage

```
minvGauss(order, nu, lambda)
levinvGauss(limit, nu, lambda, order = 1)
mgfinvGauss(x, nu, lambda, log= FALSE)
```

```
minvgauss(order, nu, lambda)
levinvgauss(limit, nu, lambda, order = 1)
mgfingauss(x, nu, lambda, log= FALSE)
```

Arguments

order	order of the moment. Only order = 1 is supported by levinvGauss.
limit	limit of the loss variable.
nu, lambda	parameters. Must be strictly positive.
x	numeric vector.
log	logical; if TRUE, the cumulant generating function is returned.

Details

The k th raw moment of the random variable X is $E[X^k]$, the k th limited moment at some limit d is $E[\min(X, d)^k]$ and the moment generating function is $E[e^{xX}]$.

The moment generating function is defined for $x \leq \lambda/(2 * \nu^2)$.

Value

minvGauss gives the k th raw moment, levinvGauss gives the k th moment of the limited loss variable, and mgfinvGauss gives the moment generating function in x .

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Christophe Dutang

References

Chhikara, R. S. and Folk, T. L. (1989), *The Inverse Gaussian Distribution: Theory, Methodology and Applications*, Decker.

Seshadri, D. N. (1989), *The Inverse Gaussian Distribution: Statistical Theory and Applications*, Springer.

See Also

[invGauss](#) in package **SuppDists** for the density function, distribution function, quantile function and random number generator.

Examples

```
minvGauss(2, 3, 4)
levinvGauss(10, 3, 4)
mgfinvGauss(0.2, 3, 4)
```

Loggamma

*The Loggamma Distribution***Description**

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Loggamma distribution with parameters `shapelog` and `ratelog`.

Usage

```
dlgamma(x, shapelog, ratelog, log = FALSE)
plgamma(q, shapelog, ratelog, lower.tail = TRUE, log.p = FALSE)
qlgamma(p, shapelog, ratelog, lower.tail = TRUE, log.p = FALSE)
rlgamma(n, shapelog, ratelog)
mlgamma(order, shapelog, ratelog)
levlgamma(limit, shapelog, ratelog, order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shapelog, ratelog</code>	parameters. Must be strictly positive.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Loggamma distribution with parameters `shapelog` = α and `ratelog` = λ has density:

$$f(x) = \frac{\lambda^\alpha}{\Gamma(\alpha)} \frac{(\log x)^{\alpha-1}}{x^{\lambda+1}}$$

for $x > 1$, $\alpha > 0$ and $\lambda > 0$. (Here $\Gamma(\alpha)$ is the function implemented by R's `gamma()` and defined in its help.)

The Loggamma is the distribution of the random variable e^X , where X has a Gamma distribution with shape parameter *alpha* and scale parameter $1/\lambda$.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

dlgamma gives the density, plgamma gives the distribution function, qlgamma gives the quantile function, rlgamma generates random deviates, mlgamma gives the k th raw moment, and levlgamma gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Hogg, R. V. and Klugman, S. A. (1984), *Loss Distributions*, Wiley.

Examples

```
exp(dlgamma(2, 3, 4, log = TRUE))
p <- (1:10)/10
plgamma(qlgamma(p, 2, 3), 2, 3)
mlgamma(2, 3, 4) - mlgamma(1, 3, 4)^2
levlgamma(10, 3, 4, order = 2)
```

Loglogistic

The Loglogistic Distribution

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Loglogistic distribution with parameters shape and scale.

Usage

```
dllogis(x, shape, rate = 1, scale = 1/rate, log = FALSE)
pllogis(q, shape, rate = 1, scale = 1/rate,
        lower.tail = TRUE, log.p = FALSE)
qllogis(p, shape, rate = 1, scale = 1/rate,
        lower.tail = TRUE, log.p = FALSE)
rllogis(n, shape, rate = 1, scale = 1/rate)
mllogis(order, shape, rate = 1, scale = 1/rate)
levllogis(limit, shape, rate = 1, scale = 1/rate,
          order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape, scale</code>	parameters. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Loglogistic distribution with parameters $\text{shape} = \gamma$ and $\text{scale} = \theta$ has density:

$$f(x) = \frac{\gamma(x/\theta)^\gamma}{x[1 + (x/\theta)^\gamma]^2}$$

for $x > 0$, $\gamma > 0$ and $\theta > 0$.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`dlogis` gives the density, `pllogis` gives the distribution function, `qllogis` gives the quantile function, `rllogis` generates random deviates, `mllogis` gives the k th raw moment, and `levllogis` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Also known as the Fisk distribution.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dllogis(2, 3, 4, log = TRUE))
p <- (1:10)/10
pllogis(qllogis(p, 2, 3), 2, 3)
mllogis(1, 2, 3)
levllogis(10, 2, 3, order = 1)
```

LognormalMoments

Raw and Limited Moments of the Lognormal Distribution

Description

Raw moments and limited moments for the lognormal distribution whose logarithm has mean equal to meanlog and standard deviation equal to sdlog.

Usage

```
mlnorm(order, meanlog = 0, sdlog = 1)
levlnorm(limit, meanlog = 0, sdlog = 1, order = 1)
```

Arguments

order	order of the moment.
limit	limit of the loss variable.
meanlog, sdlog	mean and standard deviation of the distribution on the log scale with default values of 0 and 1 respectively.

Value

mlnorm gives the k th raw moment and levlnorm gives the k th moment of the limited loss variable. Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

See Also

[Lognormal](#) for details on the lognormal distribution and functions {d,p,q,r}lnorm.

Examples

```
mlnorm(2, 3, 4) - mlnorm(1, 3, 4)^2
levlnorm(10, 3, 4, order = 2)
```

 mde *Minimum Distance Estimation*

Description

Minimum distance fitting of univariate distributions, allowing parameters to be held fixed if desired.

Usage

```
mde(x, fun, start, measure = c("CvM", "chi-square", "LAS"),
    weights = NULL, ...)
```

Arguments

x	a vector or an object of class "grouped data" (in which case only the first column of frequencies is used).
fun	function returning a cumulative distribution (for measure = "CvM" and measure = "chi-square") or a limited expected value (for measure = "LAS") evaluated at its first argument.
start	a named list giving the parameters to be optimized with initial values
measure	either "CvM" for the Cramer-von Mises method, "chi-square" for the modified chi-square method, or "LAS" for the layer average severity method.
weights	weights; see details.
...	Additional parameters, either for fun or for optim. In particular, it can be used to specify bounds via lower or upper or both. If arguments of fun are included they will be held fixed.

Details

The Cramer-von Mises method ("CvM") minimizes the squared difference between the theoretical cdf and the empirical cdf at the data points (for individual data) or the ogive at the knots (for grouped data).

The modified chi-square method ("chi-square") minimizes the modified chi-square statistic for grouped data, that is the squared difference between the expected and observed frequency within each group.

The layer average severity method ("LAS") minimizes the squared difference between the theoretical and empirical limited expected value within each group for grouped data.

All sum of squares can be weighted. If arguments weights is missing, weights default to 1 for measure = "CvM" and measure = "LAS"; for measure = "chi-square", weights default to $1/n_j$, where n_j is the frequency in group $j = 1, \dots, r$.

Optimization is performed using `optim`. For one-dimensional problems the Nelder-Mead method is used and for multi-dimensional problems the BFGS method, unless arguments named lower or upper are supplied when L-BFGS-B is used or method is supplied explicitly.

Value

An object of class "mde", a list with two components:

estimate	the parameter estimates, and
distance	the distance.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

Examples

```
## Individual data example
data(dental)
mde(dental, pexp, start = list(rate = 1/200), measure = "CvM")

## Example 2.21 of Klugman et al. (1998)
data(gdental)
mde(gdental, pexp, start = list(rate = 1/200), measure = "CvM")
mde(gdental, pexp, start = list(rate = 1/200), measure = "chi-square")
mde(gdental, levexp, start = list(rate = 1/200), measure = "LAS")

## Two-parameter distribution example
try(mde(gdental, ppareto, start = list(shape = 3, scale = 600),
       measure = "CvM")) # no convergence

## Working in log scale often solves the problem
pparetolog <- function(x, shape, scale)
  ppareto(x, exp(shape), exp(scale))

( p <- mde(gdental, pparetolog, start = list(shape = log(3),
      scale = log(600)), measure = "CvM") )
exp(p$estimate)
```

mean.grouped.data *Arithmetic Mean*

Description

Mean of grouped data objects.

Usage

```
## S3 method for class 'grouped.data'
mean(x, ...)
```

Arguments

x an object of class "grouped.data".
... further arguments passed to or from other methods.

Details

The mean of grouped data with group boundaries c_1, \dots, c_r and group frequencies n_1, \dots, n_r is

$$\sum_{j=1}^r \frac{c_{j-1} + c_j}{2} n_j.$$

Value

A named vector of means.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

See Also

[grouped.data](#) to create grouped data objects; [emm](#) to compute higher moments.

Examples

```
data(gdental)
mean(gdental)
```

NormalSupp

Moments and Moment generating function of the Normal Distribution

Description

Raw moments and moment generating function for the normal distribution with mean equal to mean and standard deviation equal to sd.

Usage

```
mnorm(order, mean = 0, sd = 1)
mgfnorm(x, mean = 0, sd = 1, log = FALSE)
```

Arguments

order	vector of integers; order of the moment.
mean	vector of means.
sd	vector of standard deviations.
x	numeric vector.
log	logical; if TRUE, the cumulant generating function is returned.

Details

The k th raw moment of the random variable X is $E[X^k]$ and the moment generating function is $E[e^{xX}]$.

Only integer moments are supported.

Value

`mnorm` gives the k th raw moment and `mgfnorm` gives the moment generating function in x .

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Christophe Dutang

References

Johnson, N. L. and Kotz, S. (1970), *Continuous Univariate Distributions, Volume 1*, Wiley.

See Also

[Normal](#)

Examples

```
mgfnorm(0:4, 1, 2)
mnorm(3)
```

ogive

Ogive for Grouped Data

Description

Compute a smoothed empirical distribution function for grouped data.

Usage

```
ogive(x, y = NULL, ...)

## S3 method for class 'ogive'
print(x, digits = getOption("digits") - 2, ...)

## S3 method for class 'ogive'
summary(object, ...)

## S3 method for class 'ogive'
knots(Fn, ...)

## S3 method for class 'ogive'
plot(x, main = NULL, xlab = "x", ylab = "F(x)", ...)
```

Arguments

x	an object of class "grouped.data" or a vector of group boundaries in ogive; for the methods, an object of class "ogive", typically.
y	a vector of group frequencies; used only if x does not inherit from class "grouped.data".
digits	number of significant digits to use, see print .
Fn, object	an R object inheriting from "ogive".
main	main title.
xlab, ylab	labels of x and y axis.
...	arguments to be passed to subsequent methods.

Details

The ogive is a linear interpolation of the empirical cumulative distribution function.

The equation of the ogive is

$$G_n(x) = \frac{(c_j - x)F_n(c_{j-1}) + (x - c_{j-1})F_n(c_j)}{c_j - c_{j-1}}$$

for $c_{j-1} < x \leq c_j$ and where c_0, \dots, c_r are the $r + 1$ group boundaries and F_n is the empirical distribution function of the sample.

Value

For ogive, a function of class "ogive", inheriting from the "function" class.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (1998), *Loss Models, From Data to Decisions*, Wiley.

See Also

[grouped.data](#) to create grouped data objects; [quantile.grouped.data](#) for the inverse function; [approxfun](#), which is used to compute the ogive; [stepfun](#) for related documentation (even though the ogive is not a step function).

Examples

```
data(gdental)
Fn <- ogive(gdental)
Fn
summary(Fn)
knots(Fn)          # the group boundaries

Fn(knots(Fn))      # true values of the empirical cdf
Fn(c(80, 200, 2000)) # linear interpolations

plot(Fn)
```

 Paralogistic

The Paralogistic Distribution

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Paralogistic distribution with parameters shape and scale.

Usage

```
dparalogis(x, shape, rate = 1, scale = 1/rate, log = FALSE)
pparalogis(q, shape, rate = 1, scale = 1/rate,
            lower.tail = TRUE, log.p = FALSE)
qparalogis(p, shape, rate = 1, scale = 1/rate,
            lower.tail = TRUE, log.p = FALSE)
rparalogis(n, shape, rate = 1, scale = 1/rate)
mparalogis(order, shape, rate = 1, scale = 1/rate)
levparalogis(limit, shape, rate = 1, scale = 1/rate,
              order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape, scale</code>	parameters. Must be strictly positive.
<code>rate</code>	an alternative way to specify the scale.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Paralogistic distribution with parameters $\text{shape} = \alpha$ and $\text{scale} = \theta$ has density:

$$f(x) = \frac{\alpha^2 (x/\theta)^\alpha}{x[1 + (x/\theta)^\alpha]^{\alpha+1}}$$

for $x > 0$, $\alpha > 0$ and $\theta > 0$.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`dparalogis` gives the density, `pparalogis` gives the distribution function, `qparalogis` gives the quantile function, `rparalogis` generates random deviates, `mparalogis` gives the k th raw moment, and `levparalogis` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dparalogis(2, 3, 4, log = TRUE))
p <- (1:10)/10
pparalogis(qparalogis(p, 2, 3), 2, 3)
mparalogis(2, 2, 3) - mparalogis(1, 2, 3)^2
levparalogis(10, 2, 3, order = 2)
```

Pareto

*The Pareto Distribution***Description**

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Pareto distribution with parameters shape and scale.

Usage

```
dpareto(x, shape, scale, log = FALSE)
ppareto(q, shape, scale, lower.tail = TRUE, log.p = FALSE)
qpareto(p, shape, scale, lower.tail = TRUE, log.p = FALSE)
rpareto(n, shape, scale)
mpareto(order, shape, scale)
levpareto(limit, shape, scale, order = 1)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If <code>length(n) > 1</code> , the length is taken to be the number required.
<code>shape, scale</code>	parameters. Must be strictly positive.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>order</code>	order of the moment.
<code>limit</code>	limit of the loss variable.

Details

The Pareto distribution with parameters $\text{shape} = \alpha$ and $\text{scale} = \theta$ has density:

$$f(x) = \frac{\alpha\theta^\alpha}{(x + \theta)^{\alpha+1}}$$

for $x > 0$, $\alpha > 0$ and θ .

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`dpareto` gives the density, `ppareto` gives the distribution function, `qpareto` gives the quantile function, `rpareto` generates random deviates, `mpareto` gives the k th raw moment, and `levpareto` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Distribution also known as the Pareto Type II or Lomax distribution.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dpareto(2, 3, 4, log = TRUE))
p <- (1:10)/10
ppareto(qpareto(p, 2, 3), 2, 3)
mpareto(1, 2, 3)
levpareto(10, 2, 3, order = 1)
```

PhaseType

The Phase-type Distribution

Description

Density, distribution function, random generation, raw moments and moment generating function for the (continuous) Phase-type distribution with parameters prob and rates.

Usage

```
dphtype(x, prob, rates, log = FALSE)
pphtype(q, prob, rates, lower.tail = TRUE, log.p = FALSE)
rphtype(n, prob, rates)
mphtype(order, prob, rates)
mgfphtype(x, prob, rates, log = FALSE)
```

Arguments

x, q	vector of quantiles.
n	number of observations. If length(n) > 1, the length is taken to be the number required.
prob	vector of initial probabilities for each of the transient states of of the underlying Markov chain. The initial probability of the absorbing state is 1 - sum(prob).
rates	square matrix of the rates of transition among the states of the underlying Markov chain.
log, log.p	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
order	order of the moment.

Details

The phase-type distribution with parameters $\text{prob} = \pi$ and rates $= \mathbf{T}$ has density:

$$f(x) = \pi e^{\mathbf{T}x} \mathbf{t}$$

for $x > 0$ and $f(0) = 1 - \pi \mathbf{e}$, where \mathbf{e} is a column vector with all components equal to one, $\mathbf{t} = -\mathbf{T}\mathbf{e}$ is the exit rates vector and $e^{\mathbf{T}x}$ denotes the matrix exponential of $\mathbf{T}x$. The matrix exponential of a matrix \mathbf{M} is defined as the Taylor series

$$e^{\mathbf{M}} = \sum_{n=0}^{\infty} \frac{\mathbf{M}^n}{n!}.$$

The parameters of the distribution must satisfy $\pi \mathbf{e} \leq 1$, $\mathbf{T}_{ii} < 0$, $\mathbf{T}_{ij} \geq 0$ and $\mathbf{T}\mathbf{e} \leq 0$.

The k th raw moment of the random variable X is $E[X^k]$ and the moment generating function is $E[e^{xX}]$.

Value

`dphasetype` gives the density, `pphasetype` gives the distribution function, `rphasetype` generates random deviates, `mphasetype` gives the k th raw moment, and `mgfpasetype` gives the moment generating function in x .

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Christophe Dutang

References

http://en.wikipedia.org/wiki/Phase-type_distribution

Neuts, M. F. (1981), *Generating random variates from a distribution of phase type*, WSC '81: Proceedings of the 13th conference on Winter simulation, IEEE Press.

Examples

```
## Erlang(3, 2) distribution
T <- cbind(c(-2, 0, 0), c(2, -2, 0), c(0, 2, -2))
pi <- c(1,0,0)
x <- 0:10

dphtype(x, pi, T) # density
dgamma(x, 3, 2) # same
pphtype(x, pi, T) # cdf
pgamma(x, 3, 2) # same

rphtype(10, pi, T) # random values

mphtype(1, pi, T) # expected value

curve(mgfphtype(x, pi, T), from = -10, to = 1)
```

`quantile.aggregateDist`*Quantiles of Aggregate Claim Amount Distribution*

Description

Quantile and Value-at-Risk methods for objects of class "aggregateDist".

Usage

```
## S3 method for class 'aggregateDist'
quantile(x,
         probs = c(0.25, 0.5, 0.75, 0.9, 0.95, 0.975, 0.99, 0.995),
         smooth = FALSE, names = TRUE, ...)

## S3 method for class 'aggregateDist'
VaR(x, conf.level = c(0.9, 0.95, 0.99),
    smooth = FALSE, names = TRUE, ...)
```

Arguments

<code>x</code>	an object of class "aggregateDist".
<code>probs, conf.level</code>	numeric vector of probabilities with values in $[0, 1)$.
<code>smooth</code>	logical; when TRUE and <code>x</code> is a step function, quantiles are linearly interpolated between knots.
<code>names</code>	logical; if true, the result has a <code>names</code> attribute. Set to FALSE for speedup with many <code>probs</code> .
<code>...</code>	further arguments passed to or from other methods.

Details

The quantiles are taken directly from the cumulative distribution function defined in `x`. Linear interpolation is available for step functions.

Value

A numeric vector, named if `names` is TRUE.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Louis-Philippe Pouliot

See Also

[aggregateDist](#)

Examples

```

model.freq <- expression(data = rpois(3))
model.sev <- expression(data = rlnorm(10, 1.5))
Fs <- aggregateDist("simulation", model.freq, model.sev, nb.simul = 1000)
quantile(Fs, probs = c(0.25, 0.5, 0.75))
VaR(Fs)

```

quantile.grouped.data *Quantiles of Grouped Data*

Description

Sample quantiles corresponding to the given probabilities for objects of class "grouped.data".

Usage

```

## S3 method for class 'grouped.data'
quantile(x, probs = seq(0, 1, 0.25),
        names = TRUE, ...)

```

Arguments

x	an object of class "grouped.data".
probs	numeric vector of probabilities with values in [0, 1].
names	logical; if true, the result has a names attribute. Set to FALSE for speedup with many probs.
...	further arguments passed to or from other methods.

Details

The quantile function is the inverse of the ogive, that is a linear interpolation of the empirical quantile function.

The equation of the quantile function is

$$x = \frac{c_j(F_n(c_{j-1}) - q) + c_{j-1}(q - F_n(c_j))}{F_n(c_j) - F_n(c_{j-1})}$$

for $0 \leq q \leq c_j$ and where c_0, \dots, c_r are the $r + 1$ group boundaries and F_n is the empirical distribution function of the sample.

Value

A numeric vector, named if names is TRUE.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>

See Also

[ogive](#) for the smoothed empirical distribution of which `quantile.grouped.data` is an inverse; [grouped.data](#) to create grouped data objects.

Examples

```
data(gdental)
quantile(gdental)
Fn <- ogive(gdental)
Fn(quantile(gdental)) # inverse function
```

ruin	<i>Probability of Ruin</i>
------	----------------------------

Description

Calculation of infinite time probability of ruin in the models of Cramér-Lundberg and Sparre Andersen, that is with exponential or phase-type (including mixtures of exponentials, Erlang and mixture of Erlang) claims interarrival time.

Usage

```
ruin(claims = c("exponential", "Erlang", "phase-type"), par.claims,
     wait = c("exponential", "Erlang", "phase-type"), par.wait,
     premium.rate = 1, tol = sqrt(.Machine$double.eps),
     maxit = 200, echo = FALSE)
```

```
## S3 method for class 'ruin'
plot(x, from = NULL, to = NULL, add = FALSE,
     xlab = "u", ylab = expression(psi(u)),
     main = "Probability of Ruin", xlim = NULL, ...)
```

Arguments

<code>claims</code>	character; the type of claim severity distribution.
<code>wait</code>	character; the type of claim interarrival (wait) time distribution.
<code>par.claims</code> , <code>par.wait</code>	named list containing the parameters of the distribution (see details).
<code>premium.rate</code>	numeric vector of length 1; the premium rate.
<code>tol</code> , <code>maxit</code> , <code>echo</code>	respectively the tolerance level of the stopping criteria, the maximum number of iterations and whether or not to echo the procedure when the transition rates matrix is determined iteratively. Ignored if <code>wait = "exponential"</code> .
<code>x</code>	an object of class "ruin".
<code>from</code> , <code>to</code>	the range over which the function will be plotted.

add	logical; if TRUE add to already existing plot.
xlim	numeric of length 2; if specified, it serves as default for c(from, to).
xlab, ylab	label of the x and y axes, respectively.
main	main title.
...	further graphical parameters accepted by <code>curve</code> .

Details

The names of the parameters in `par.claims` and `par.wait` must be the same as in `dexp`, `dgamma` or `dphtype`, as appropriate. A model will be a mixture of exponential or Erlang distributions (but not phase-type) when the parameters are vectors of length > 1 and the parameter list contains a vector of weights of the coefficients of the mixture.

Parameters are recycled when needed. Their names can be abbreviated.

Combinations of exponentials as defined in Dufresne and Gerber (1988) are *not* supported.

Ruin probabilities are evaluated using `pphtype` except when both distributions are exponential, in which case an explicit formula is used.

When `wait != "exponential"` (Sparre Andersen model), the transition rate matrix Q of the distribution of the probability of ruin is determined iteratively using a fixed point-like algorithm. The stopping criteria used is

$$\max \left\{ \sum_{j=1}^n |Q_{ij} - Q'_{ij}| \right\} < \text{tol},$$

where Q and Q' are two successive values of the matrix.

Value

A function of class "ruin" inheriting from the "function" class to compute the probability of ruin given initial surplus levels. The function has arguments:

u	numeric vector of initial surplus levels;
survival	logical; if FALSE (default), probabilities are $\psi(u)$, otherwise, $\phi(u) = 1 - \psi(u)$;
lower.tail	an alias for !survival.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, and Christophe Dutang

References

Asmussen, S. and Rolski, T. (1991), Computational methods in risk theory: A matrix algorithmic approach, *Insurance: Mathematics and Economics* **10**, 259–274.

Dufresne, F. and Gerber, H. U. (1988), Three methods to calculate the probability of ruin, *Astin Bulletin* **19**, 71–90.

Gerber, H. U. (1979), *An Introduction to Mathematical Risk Theory*, Huebner Foundation.

Examples

```

## Case with an explicit formula: exponential claims and exponential
## interarrival times.
psi <- ruin(claims = "e", par.claims = list(rate = 5),
           wait   = "e", par.wait   = list(rate = 3))

psi
psi(0:10)
plot(psi, from = 0, to = 10)

## Mixture of two exponentials for claims, exponential interarrival
## times (Gerber 1979)
psi <- ruin(claims = "e", par.claims = list(rate = c(3, 7), w = 0.5),
           wait   = "e", par.wait   = list(rate = 3), pre = 1)

u <- 0:10
psi(u)
(24 * exp(-u) + exp(-6 * u))/35 # same

## Phase-type claims, exponential interarrival times (Asmussen and
## Rolski 1991)
p <- c(0.5614, 0.4386)
r <- matrix(c(-8.64, 0.101, 1.997, -1.095), 2, 2)
lambda <- 1/(1.1 * mphtype(1, p, r))
psi <- ruin(claims = "p", par.claims = list(prob = p, rates = r),
           wait   = "e", par.wait   = list(rate = lambda))

psi
plot(psi, xlim = c(0, 50))

## Phase-type claims, mixture of two exponentials for interarrival times
## (Asmussen and Rolski 1991)
a <- (0.4/5 + 0.6) * lambda
ruin(claims = "p", par.claims = list(prob = p, rates = r),
     wait   = "e", par.wait   = list(rate = c(5 * a, a), weights =
                                     c(0.4, 0.6)),
     maxit = 225)

```

severity

Manipulation of Individual Claim Amounts

Description

severity is a generic function created to manipulate individual claim amounts. The function invokes particular *methods* which depend on the `class` of the first argument.

Usage

```

severity(x, ...)

## Default S3 method:
severity(x, bycol = FALSE, drop = TRUE, ...)

```

Arguments

x	an R object.
bycol	logical; whether to “unroll” horizontally (FALSE) or vertically (TRUE)
...	further arguments to be passed to or from other methods.
drop	logical; if TRUE, the result is coerced to the lowest possible dimension.

Details

Currently, the default method is equivalent to [unroll](#). This is liable to change since the link between the name and the use of the function is rather weak.

Value

A vector or matrix.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Louis-Philippe Pouliot

See Also

[severity.portfolio](#) for the original motivation of these functions.

Examples

```
x <- list(c(1:3), c(1:8), c(1:4), c(1:3))
(mat <- matrix(x, 2, 2))
severity(mat)
severity(mat, bycol = TRUE)
```

simul

Simulation from Compound Hierarchical Models

Description

simul simulates data for insurance applications allowing hierarchical structures and separate models for the frequency and severity of claims distributions.

Usage

```
simul(nodes, model.freq = NULL, model.sev = NULL, weights = NULL)
```

```
## S3 method for class 'portfolio'
print(x, ...)
```

Arguments

nodes	a named list giving the number of "nodes" at each level in the hierarchy of the portfolio. The nodes are listed from top (portfolio) to bottom (usually the years of experience).
model.freq	a named vector of expressions specifying the frequency of claims model (see details); if NULL, only claim amounts are simulated.
model.sev	a named vector of expressions specifying the severity of claims model (see details); if NULL, only claim numbers are simulated.
weights	a vector of weights.
x	a portfolio object.
...	potential further arguments required by generic.

Details

The order and the names of the elements in nodes, model.freq and model.sev must match. At least one of model.freq and model.sev must be non NULL.

nodes specifies the hierarchical layout of the portfolio. Each element of the list is a vector of the number of nodes at a given level. Vectors are recycled as necessary.

model.freq and model.sev specify the simulation models for claim numbers and claim amounts, respectively. A model is expressed in a semi-symbolic fashion using an object of mode [expression](#). Each element of the object must be named and should be a complete call to a random number generation function, with the number of variates omitted. Hierarchical (or mixtures of) models are achieved by replacing one or more parameters of a distribution at a given level by any combination of the names of the levels above. If no mixing is to take place at a level, the model for this level can be NULL.

The argument of the random number generation functions for the number of variates to simulate **must** be named n.

Weights will be used wherever the name "weights" appears in a model. It is the user's responsibility to ensure that the length of weights will match the number of nodes when weights are to be used. Normally, there should be one weight per node at the lowest level of the model.

Data is generated in lexicographic order, that is by row in the output matrix.

Value

An object of class "portfolio". A print method for this class displays the models used in the simulation as well as the frequency of claims for each year and entity in the portfolio.

An object of class "portfolio" is a list containing the following components:

data	a two dimension list where each element is a vector of claim amounts;
weights	the vector of weights given in argument reshaped as a matrix matching element data, or NULL;
classification	a matrix of integers where each row is a unique set of subscripts identifying an entity in the portfolio (e.g. integers i, j and k for data X_{ijkt});
nodes	the nodes argument, appropriately recycled;

model.freq the frequency model as given in argument;
 model.sev the severity model as given in argument.

It is recommended to manipulate objects of class "portfolio" by means of the corresponding methods of functions aggregate, frequency and severity.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Sébastien Auclair and Louis-Philippe Pouliot

References

Goulet, V. and Pouliot, L.-P. (2008), Simulation of compound hierarchical models in R, *North American Actuarial Journal* **12**, 401–412.

See Also

[simul.summaries](#) for the functions to create the matrices of aggregate claim amounts, frequencies and individual claim amounts.

Examples

```
## Simple two level (contracts and years) portfolio with frequency model
## Nit|Theta_i ~ Poisson(Theta_i), Theta_i ~ Gamma(2, 3) and severity
## model X ~ Lognormal(5, 1)
simul(nodes = list(contract = 10, year = 5),
      model.freq = expression(contract = rgamma(2, 3),
                             year = rpois(contract)),
      model.sev = expression(contract = NULL,
                             year = rlnorm(5, 1)))

## Model with weights and mixtures for both frequency and severity
## models
nodes <- list(entity = 8, year = c(5, 4, 4, 5, 3, 5, 4, 5))
mf <- expression(entity = rgamma(2, 3),
                year = rpois(weights * entity))
ms <- expression(entity = rnorm(5, 1),
                year = rlnorm(entity, 1))
wit <- sample(2:10, 35, replace = TRUE)
pf <- simul(nodes, mf, ms, wit)
pf # print method
weights(pf) # extraction of weights
aggregate(pf)[, -1]/weights(pf)[, -1] # ratios

## Four level hierarchical model for frequency only
nodes <- list(sector = 3, unit = c(3, 4),
             employer = c(3, 4, 3, 4, 2, 3, 4), year = 5)
mf <- expression(sector = rexp(1),
                unit = rexp(sector),
                employer = rgamma(unit, 1),
                year = rpois(employer))
pf <- simul(nodes, mf, NULL)
```

```

pf # print method
aggregate(pf) # aggregate claim amounts
frequency(pf) # frequencies
severity(pf) # individual claim amounts

```

simul.summaries *Summary Statistics of a Portfolio*

Description

Methods for [class](#) "portfolio" objects.

aggregate splits portfolio data into subsets and computes summary statistics for each.

frequency computes the frequency of claims for subsets of portfolio data.

severity extracts the individual claim amounts.

weights extracts the matrix of weights.

Usage

```

## S3 method for class 'portfolio'
aggregate(x, by = names(x$nodes), FUN = sum,
          classification = TRUE, prefix = NULL, ...)

## S3 method for class 'portfolio'
frequency(x, by = names(x$nodes),
          classification = TRUE, prefix = NULL, ...)

## S3 method for class 'portfolio'
severity(x, by = head(names(x$node), -1), splitcol = NULL,
         classification = TRUE, prefix = NULL, ...)

## S3 method for class 'portfolio'
weights(object, classification = TRUE, prefix = NULL, ...)

```

Arguments

x, object	an object of class "portfolio", typically created with simul .
by	character vector of grouping elements using the level names of the portfolio in x. The names can be abbreviated.
FUN	the function to be applied to data subsets.
classification	boolean; if TRUE, the node identifier columns are included in the output.
prefix	characters to prefix column names with; if NULL, sensible defaults are used when appropriate.
splitcol	columns of the data matrix to extract separately; usual matrix indexing methods are supported.
...	optional arguments to FUN, or passed to or from other methods.

Details

By default, `aggregate.portfolio` computes the aggregate claim amounts for the grouping specified in `by`. Any other statistic based on the individual claim amounts can be used through argument `FUN`.

`frequency.portfolio` is equivalent to using `aggregate.portfolio` with argument `FUN` equal to `if (identical(x, NA)) NA else length(x)`.

`severity.portfolio` extracts individual claim amounts of a portfolio by groupings using the default method of `severity`. Argument `splitcol` allows to get the individual claim amounts of specific columns separately.

`weights.portfolio` extracts the weight matrix of a portfolio.

Value

A matrix or vector depending on the groupings specified in `by`.

For the `aggregate` and `frequency` methods: if at least one level other than the last one is used for grouping, the result is a matrix obtained by binding the appropriate node identifiers extracted from `x$classification` if `classification = TRUE`, and the summaries per grouping. If the last level is used for grouping, the column names of `x$data` are retained; if the last level is not used for grouping, the column name is replaced by the deparsed name of `FUN`. If only the last level is used (column summaries), a named vector is returned.

For the `severity` method: a list of two elements:

<code>main</code>	NULL or a matrix of claim amounts for the columns not specified in <code>splitcol</code> , with the appropriate node identifiers extracted from <code>x\$classification</code> if <code>classification = TRUE</code> ;
<code>split</code>	same as above, but for the columns specified in <code>splitcol</code> .

For the `weights` method: the weight matrix of the portfolio with node identifiers if `classification = TRUE`.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Louis-Philippe Pouliot.

See Also

[simul](#)

Examples

```
nodes <- list(sector = 3, unit = c(3, 4),
             employer = c(3, 4, 3, 4, 2, 3, 4), year = 5)
model.freq <- expression(sector = rexp(1),
                        unit = rexp(sector),
                        employer = rgamma(unit, 1),
                        year = rpois(employer))
model.sev <- expression(sector = rnorm(6, 0.1),
                      unit = rnorm(sector, 1),
```

```

        employer = rnorm(unit, 1),
        year = rlnorm(employer, 1))
pf <- simul(nodes, model.freq, model.sev)

aggregate(pf)          # aggregate claim amount by employer and year
aggregate(pf, classification = FALSE) # same, without node identifiers
aggregate(pf, by = "sector")      # by sector
aggregate(pf, by = "y")          # by year
aggregate(pf, by = c("s", "u"), mean) # average claim amount

frequency(pf)          # number of claims
frequency(pf, prefix = "freq.") # more explicit column names

severity(pf)           # claim amounts by row
severity(pf, by = "year") # by column
severity(pf, by = c("s", "u")) # by unit
severity(pf, splitcol = "year.5") # last year separate
severity(pf, splitcol = 5) # same
severity(pf, splitcol = c(FALSE, FALSE, FALSE, FALSE, TRUE)) # same

weights(pf)

## For portfolios with weights, the following computes loss ratios.
## Not run: aggregate(pf, classif = FALSE) / weights(pf, classif = FALSE)

```

SingleParameterPareto *The Single-parameter Pareto Distribution*

Description

Density function, distribution function, quantile function, random generation, raw moments, and limited moments for the Single-parameter Pareto distribution with parameter shape.

Usage

```

dpareto1(x, shape, min, log = FALSE)
ppareto1(q, shape, min, lower.tail = TRUE, log.p = FALSE)
qpareto1(p, shape, min, lower.tail = TRUE, log.p = FALSE)
rpareto1(n, shape, min)
mpareto1(order, shape, min)
levpareto1(limit, shape, min, order = 1)

```

Arguments

x, q	vector of quantiles.
p	vector of probabilities.
n	number of observations. If length(n) > 1, the length is taken to be the number required.

shape	parameter. Must be strictly positive.
min	lower bound of the support of the distribution.
log, log.p	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
order	order of the moment.
limit	limit of the loss variable.

Details

The Single-parameter Pareto distribution with parameter $\text{shape} = \alpha$ has density:

$$f(x) = \frac{\alpha\theta^\alpha}{x^{\alpha+1}}$$

for $x > \theta$, $\alpha > 0$ and $\theta > 0$.

Although there appears to be two parameters, only shape is a true parameter. The value of $\text{min} = \theta$ must be set in advance.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`dpareto1` gives the density, `ppareto1` gives the distribution function, `qpareto1` gives the quantile function, `rpareto1` generates random deviates, `mpareto1` gives the k th raw moment, and `levpareto1` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dpareto1(5, 3, 4, log = TRUE))
p <- (1:10)/10
ppareto1(qpareto1(p, 2, 3), 2, 3)
mpareto1(2, 3, 4) - mpareto1(1, 3, 4) ^ 2
levpareto(10, 3, 4, order = 2)
```

TransformedBeta *The Transformed Beta Distribution*

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Transformed Beta distribution with parameters shape1, shape2, shape3 and scale.

Usage

```
dtrbeta(x, shape1, shape2, shape3, rate = 1, scale = 1/rate,
        log = FALSE)
ptrbeta(q, shape1, shape2, shape3, rate = 1, scale = 1/rate,
        lower.tail = TRUE, log.p = FALSE)
qtrbeta(p, shape1, shape2, shape3, rate = 1, scale = 1/rate,
        lower.tail = TRUE, log.p = FALSE)
rtrbeta(n, shape1, shape2, shape3, rate = 1, scale = 1/rate)
mtrbeta(order, shape1, shape2, shape3, rate = 1, scale = 1/rate)
levtrbeta(limit, shape1, shape2, shape3, rate = 1, scale = 1/rate,
          order = 1)
```

Arguments

x, q	vector of quantiles.
p	vector of probabilities.
n	number of observations. If length(n) > 1, the length is taken to be the number required.
shape1, shape2, shape3, scale	parameters. Must be strictly positive.
rate	an alternative way to specify the scale.
log, log.p	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
order	order of the moment.
limit	limit of the loss variable.

Details

The Transformed Beta distribution with parameters shape1 = α , shape2 = γ , shape3 = τ and scale = θ , has density:

$$f(x) = \frac{\Gamma(\alpha + \tau)}{\Gamma(\alpha)\Gamma(\tau)} \frac{\gamma(x/\theta)^{\gamma\tau}}{x[1 + (x/\theta)^\gamma]^{\alpha+\tau}}$$

for $x > 0$, $\alpha > 0$, $\gamma > 0$, $\tau > 0$ and $\theta > 0$. (Here $\Gamma(\alpha)$ is the function implemented by R's [gamma\(\)](#) and defined in its help.)

The Transformed Beta is the distribution of the random variable

$$\theta \left(\frac{X}{1-X} \right)^{1/\gamma},$$

where X has a Beta distribution with parameters τ and α .

The Transformed Beta distribution defines a family of distributions with the following special cases:

- A **Burr** distribution when `shape3 == 1`;
- A **Loglogistic** distribution when `shape1 == shape3 == 1`;
- A **Paralogistic** distribution when `shape3 == 1` and `shape2 == shape1`;
- A **Generalized Pareto** distribution when `shape2 == 1`;
- A **Pareto** distribution when `shape2 == shape3 == 1`;
- An **Inverse Burr** distribution when `shape1 == 1`;
- An **Inverse Pareto** distribution when `shape2 == shape1 == 1`;
- An **Inverse Paralogistic** distribution when `shape1 == 1` and `shape3 == shape2`.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`dtrbeta` gives the density, `ptrbeta` gives the distribution function, `qtrbeta` gives the quantile function, `rtrbeta` generates random deviates, `mtrbeta` gives the k th raw moment, and `levtrbeta` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Distribution also known as the Generalized Beta of the Second Kind and Pearson Type VI.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dtrbeta(2, 2, 3, 4, 5, log = TRUE))
p <- (1:10)/10
ptrbeta(qtrbeta(p, 2, 3, 4, 5), 2, 3, 4, 5)
qpearson6(0.3, 2, 3, 4, 5, lower.tail = FALSE)
mtrbeta(2, 1, 2, 3, 4) - mtrbeta(1, 1, 2, 3, 4) ^ 2
levtrbeta(10, 1, 2, 3, 4, order = 2)
```

 TransformedGamma *The Transformed Gamma Distribution*

Description

Density function, distribution function, quantile function, random generation, raw moments and limited moments for the Transformed Gamma distribution with parameters shape1, shape2 and scale.

Usage

```

dtrgamma(x, shape1, shape2, rate = 1, scale = 1/rate,
         log = FALSE)
ptrgamma(q, shape1, shape2, rate = 1, scale = 1/rate,
         lower.tail = TRUE, log.p = FALSE)
qtrgamma(p, shape1, shape2, rate = 1, scale = 1/rate,
         lower.tail = TRUE, log.p = FALSE)
rtrgamma(n, shape1, shape2, rate = 1, scale = 1/rate)
mtrgamma(order, shape1, shape2, rate = 1, scale = 1/rate)
levtrgamma(limit, shape1, shape2, rate = 1, scale = 1/rate,
           order = 1)
  
```

Arguments

x, q	vector of quantiles.
p	vector of probabilities.
n	number of observations. If length(n) > 1, the length is taken to be the number required.
shape1, shape2, scale	parameters. Must be strictly positive.
rate	an alternative way to specify the scale.
log, log.p	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
order	order of the moment.
limit	limit of the loss variable.

Details

The Transformed Gamma distribution with parameters shape1 = α , shape2 = τ and scale = θ has density:

$$f(x) = \frac{\tau u^\alpha e^{-u}}{x \Gamma(\alpha)}, \quad u = (x/\theta)^\tau$$

for $x > 0$, $\alpha > 0$, $\tau > 0$ and $\theta > 0$. (Here $\Gamma(\alpha)$ is the function implemented by R's [gamma\(\)](#) and defined in its help.)

The Transformed Gamma is the distribution of the random variable $\theta X^{1/\tau}$, where X has a Gamma distribution with shape parameter α and scale parameter 1 or, equivalently, of the random variable $Y^{1/\tau}$ with Y a Gamma distribution with shape parameter α and scale parameter θ^τ .

The Transformed Gamma probability distribution defines a family of distributions with the following special cases:

- A [Gamma](#) distribution when `shape2 == 1`;
- A [Weibull](#) distribution when `shape1 == 1`;
- An [Exponential](#) distribution when `shape2 == shape1 == 1`.

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`dtrgamma` gives the density, `ptrgamma` gives the distribution function, `qtrgamma` gives the quantile function, `rtrgamma` generates random deviates, `mtrgamma` gives the k th raw moment, and `levtrgamma` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Note

Distribution also known as the Generalized Gamma.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

Examples

```
exp(dtrgamma(2, 3, 4, 5, log = TRUE))
p <- (1:10)/10
ptrgamma(qtrgamma(p, 2, 3, 4), 2, 3, 4)
mtrgamma(2, 3, 4, 5) - mtrgamma(1, 3, 4, 5) ^ 2
levtrgamma(10, 3, 4, 5, order = 2)
```

UniformSupp	<i>Moments and Moment Generating Function of the Uniform Distribution</i>
-------------	---

Description

Raw moments, limited moments and moment generating function for the Uniform distribution from min to max.

Usage

```
munif(order, min = 0, max = 1)
levunif(limit, min = 0, max = 1, order = 1)
mgfunif(x, min = 0, max = 1, log = FALSE)
```

Arguments

order	order of the moment.
min, max	lower and upper limits of the distribution. Must be finite.
limit	limit of the random variable.
x	numeric vector.
log	logical; if TRUE, the cumulant generating function is returned.

Details

The k th raw moment of the random variable X is $E[X^k]$, the k th limited moment at some limit d is $E[\min(X, d)^k]$ and the moment generating function is $E[e^{xX}]$.

Value

munif gives the k th raw moment, levunif gives the k th moment of the limited random variable, and mgfunif gives the moment generating function in x.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca>, Christophe Dutang

References

http://en.wikipedia.org/wiki/Uniform_distribution_%28continuous%29

See Also

[Uniform.](#)

Examples

```
munif(-1)
munif(1:5)
levunif(3, order=1:5)
levunif(3, 2,4)
mgfunif(1,1,2)
```

unroll

Display a Two-Dimension Version of a Matrix of Vectors

Description

Displays all values of a matrix of vectors by “unrolling” the object vertically or horizontally.

Usage

```
unroll(x, bycol = FALSE, drop = TRUE)
```

Arguments

x	a list of vectors with a <code>dim</code> attribute of length 0, 1 or 2.
bycol	logical; whether to unroll horizontally (FALSE) or vertically (TRUE).
drop	logical; if TRUE, the result is coerced to the lowest possible dimension.

Details

`unroll` returns a matrix where elements of `x` are concatenated (“unrolled”) by row (`bycol = FALSE`) or by column (`bycol = TRUE`). `NA` is used to make rows/columns of equal length.

Vectors and one dimensional arrays are coerced to **row** matrices.

Value

A vector or matrix.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Louis-Philippe Pouliot

See Also

This function was originally written for use in [severity.portfolio](#).

Examples

```
x <- list(c(1:3), c(1:8), c(1:4), c(1:3))
(mat <- matrix(x, 2, 2))

unroll(mat)
unroll(mat, bycol = TRUE)

unroll(mat[1, ])
unroll(mat[1, ], drop = FALSE)
```

VaR*Value at Risk*

Description

Value at Risk.

Usage

```
VaR(x, ...)
```

Arguments

x an R object.
... further arguments passed to or from other methods.

Details

This is a generic function with, currently, only a method for objects of class "aggregateDist".

Value

An object of class numeric.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Tommy Ouellet

See Also

[VaR.aggregateDist](#), [aggregateDist](#)

Description

Raw moments and limited moments for the Weibull distribution with parameters shape and scale.

Usage

```
mweibull(order, shape, scale = 1)
levweibull(limit, shape, scale = 1, order = 1)
```

Arguments

order order of the moment.
 limit limit of the loss variable.
 shape, scale shape and scale parameters, the latter defaulting to 1.

Details

The k th raw moment of the random variable X is $E[X^k]$ and the k th limited moment at some limit d is $E[\min(X, d)^k]$.

Value

`mweibull` gives the k th raw moment and `levweibull` gives the k th moment of the limited loss variable.

Invalid arguments will result in return value NaN, with a warning.

Author(s)

Vincent Goulet <vincent.goulet@act.ulaval.ca> and Mathieu Pigeon

References

Klugman, S. A., Panjer, H. H. and Willmot, G. E. (2008), *Loss Models, From Data to Decisions, Third Edition*, Wiley.

See Also

[Weibull](#) for details on the Weibull distribution and functions `{d,p,q,r}weibull`.

Examples

```
mweibull(2, 3, 4) - mweibull(1, 3, 4)^2
levweibull(10, 3, 4, order = 2)
```

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